

# Dihadron correlations at eRHIC and Monte Carlo development

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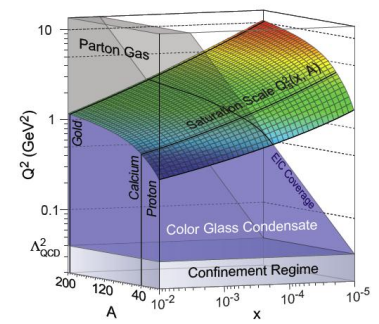
**BROOKHAVEN**  
NATIONAL LABORATORY



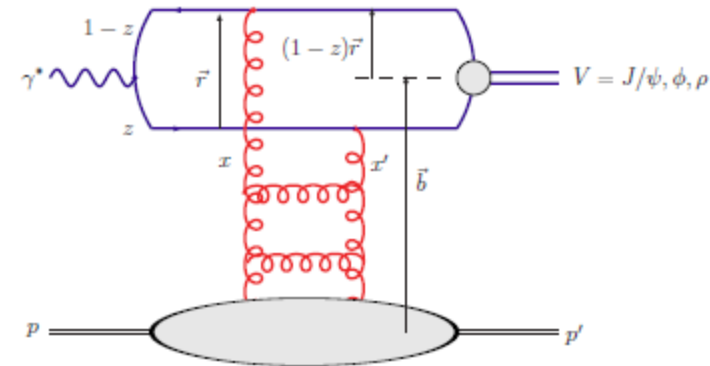
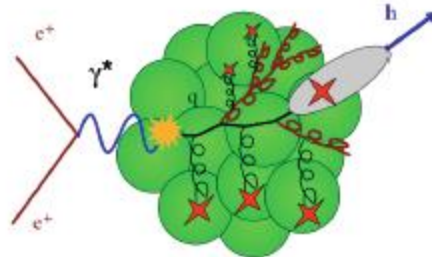
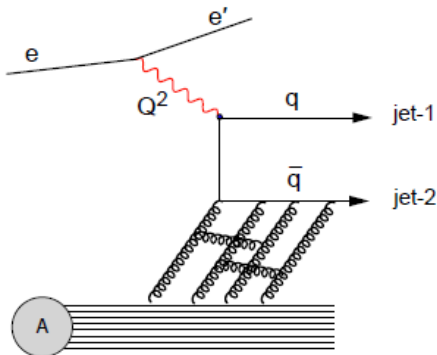
# Outline

- Motivation
- RHIC forward dAu program
- Dihadron correlation at future eRHIC
  - Monte Carlo results
  - Compared with CGC prediction
  - The power of Monte Carlo
- Summary and Prospects

# Motivation



- **eA program will investigate the nuclei structure with great precision**
  - Probing gluon dynamics, establish the existence of the saturation regime.
  - Study cold nuclear medium effect with parton propagation and hadronization in nuclear matter.
  - Image nuclear gluon structure.
- **dihadron correlation is a key measurement in the eA program to help us explore the saturation physics.**



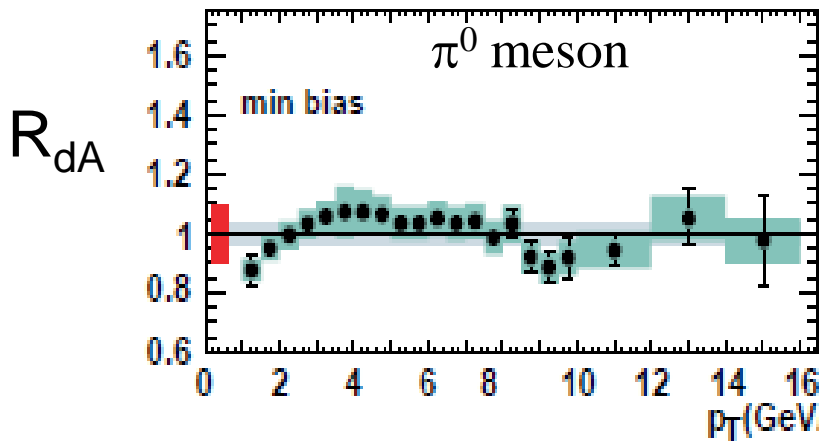
# RHIC forward dAu program

Nuclear modification factor

$$R_{dAu} \equiv \frac{1}{\langle N_{coll} \rangle} \frac{d^2 N^{d+Au} / dp_T d\eta}{d^2 N_{inel}^{p+p} / dp_T d\eta}$$

PHENIX  $|\eta| < 0.35$

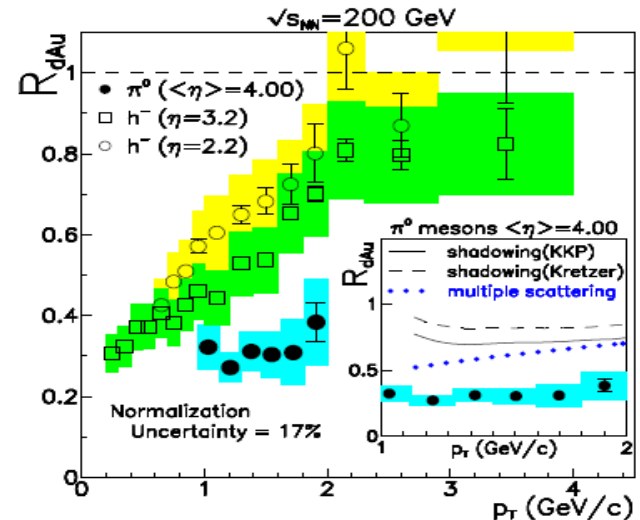
PRL 98 (2007), 172302



$R_{dA} \sim 1$  at mid rapidity

STAR, BRAHMS

PRL 97 (2006), 152302



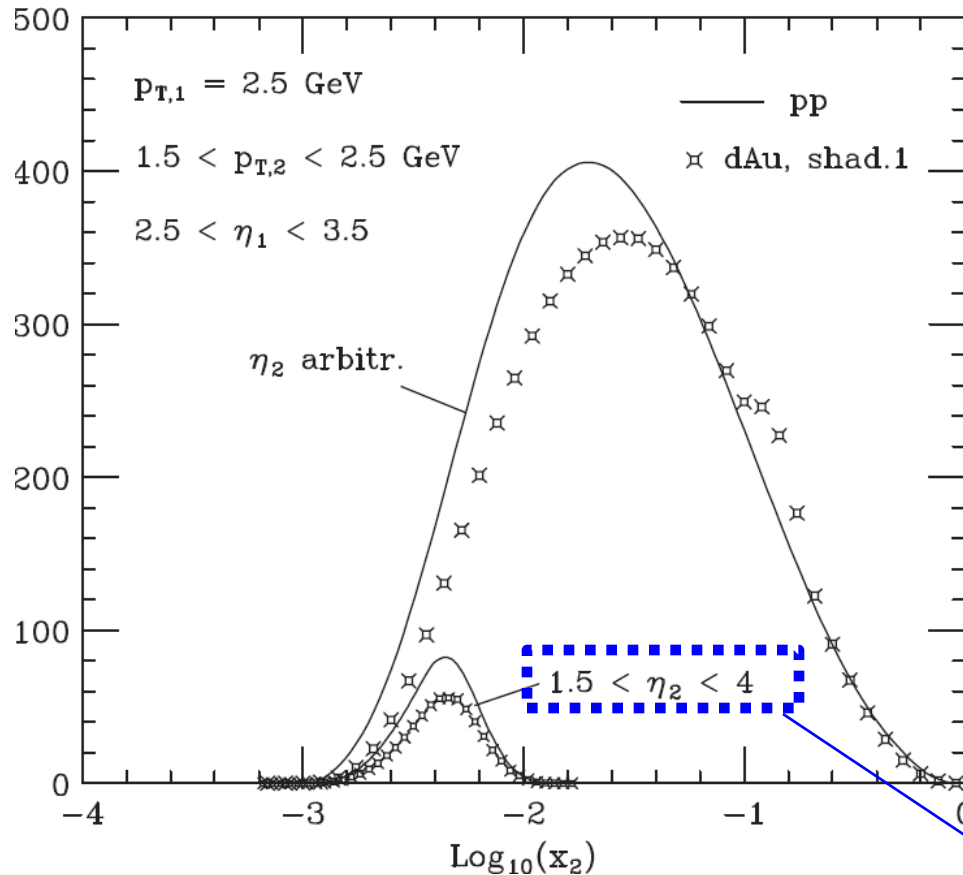
$R_{dA} < 1$ , Single hadron production  
suppressed at forward rapidity.

Cold Nuclear Matter (CNM) effect.

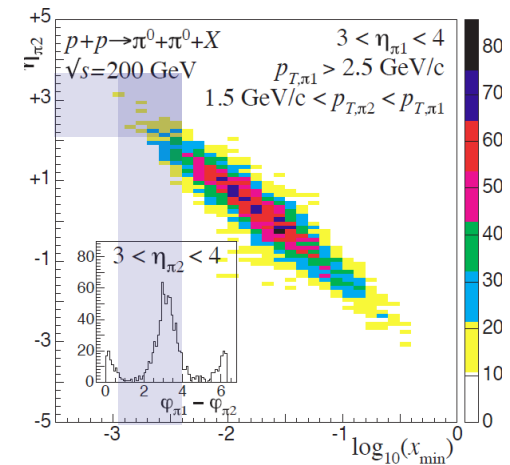
Probing small x region.  $x_2 = \frac{M_T}{\sqrt{S}} e^{-y}$

# Dihadron correlation at RHIC forward dAu program

Guzey, Strikman, Vogelsang, PL B603, 173



Eur.Phys.J.C43:427-435,2005



The rapidity of associate particle correlated with the  $x$  of struck gluon.

From the Pythia 2->2 process

Probably onset of saturation.

Constrain  $x$  range.

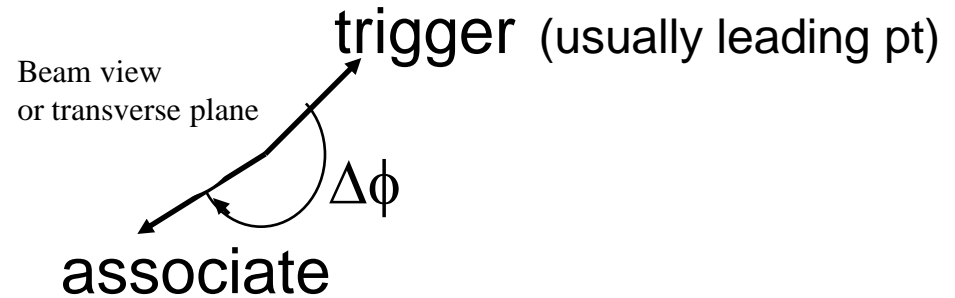
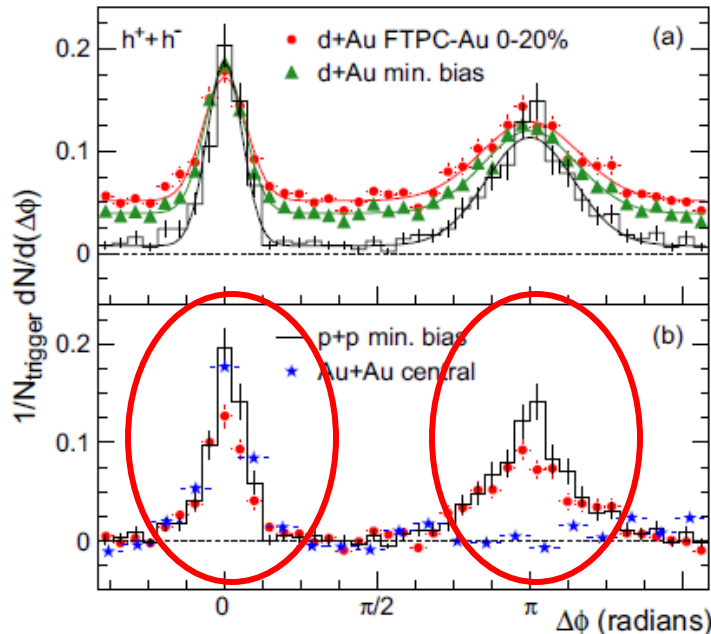
Approach to smaller mean  $x$

# Dihadron correlation measurement

CY ( Conditional Yield )

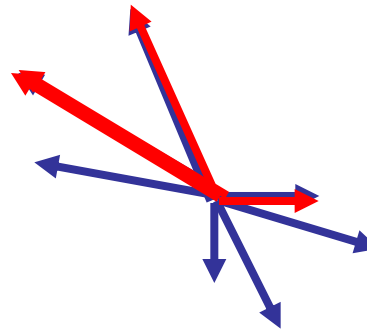
$$CY = \frac{1}{N_{trig}} \frac{dN^{assoc}}{d\Delta\phi}$$

Phys. Rev. Lett. 91 072304



**Nearside peak: delivers jet fragmentation information**

**Awayside peak: medium  $k_T$  kick both from initial and final state**



**pp dAu dihadron correlation are similar at mid rapidity, suppression in AuAu collision is dominated by final state interaction**

# Dihadron correlation measurement

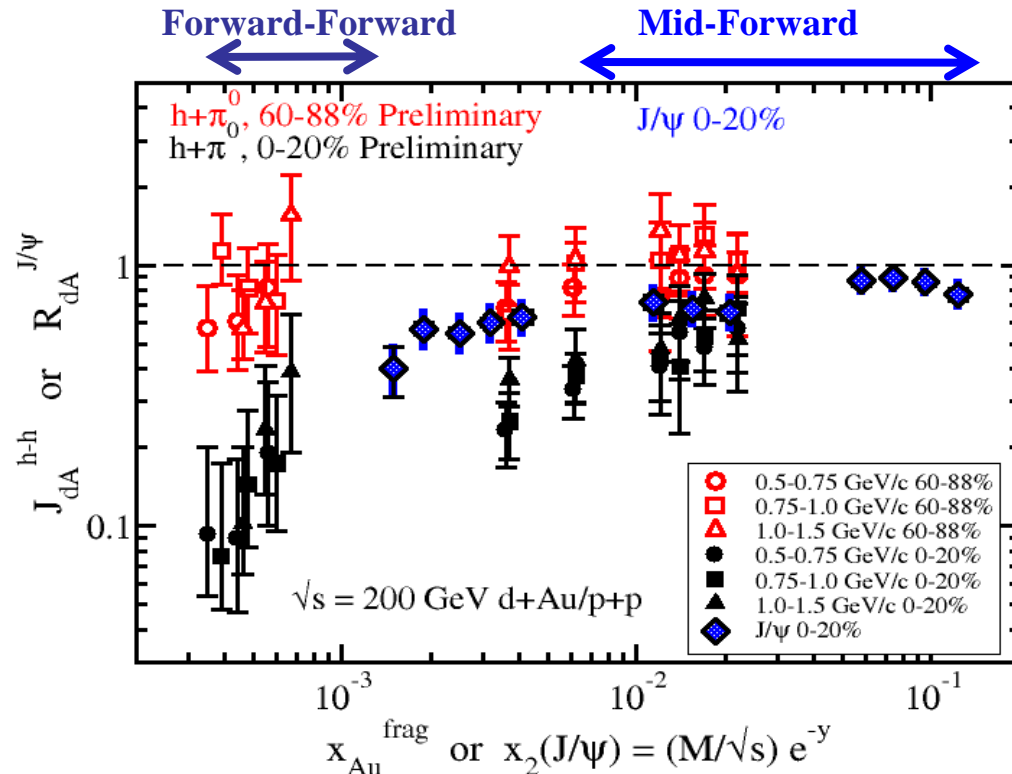
$$J_{dA} = \frac{\sigma_{dA}^{pair} / \sigma_{dA}}{\langle N_{coll} \rangle \sigma_{pp}^{pair} / \sigma_{pp}}$$

Dihadron pair nuclear modification factor

$$J_{dA} = R_{dA}^{trig} \times I_{dA}$$

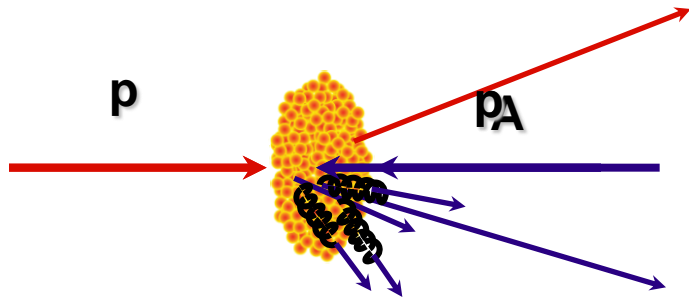
$$I_{dA} = \frac{CY_{dA}}{CY_{pp}}$$

PHENIX arXiv:1109.2133v1



# Dihadron correlation at RHIC forward dAu program

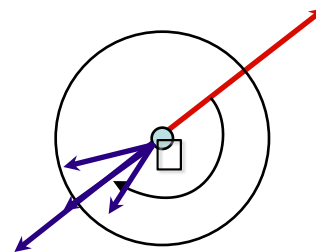
side-view



**Low gluon density (pp):**  
pQCD predicts  $2 \rightarrow 2$  process  
 $\Rightarrow$  back-to-back di-jet

**High gluon density (pA):**  
 $2 \rightarrow$  many process  
 $\Rightarrow$  expect broadening of away-side

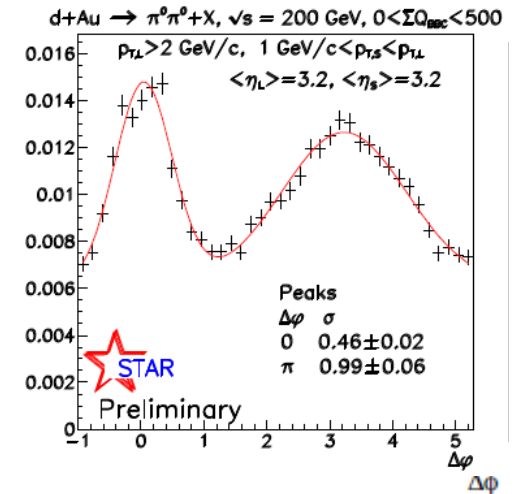
beam-view



Multiple emissions de-correlate the away side peak for forward-forward di-pion correlation.

Gluon densities saturate first in the center of the nucleus.

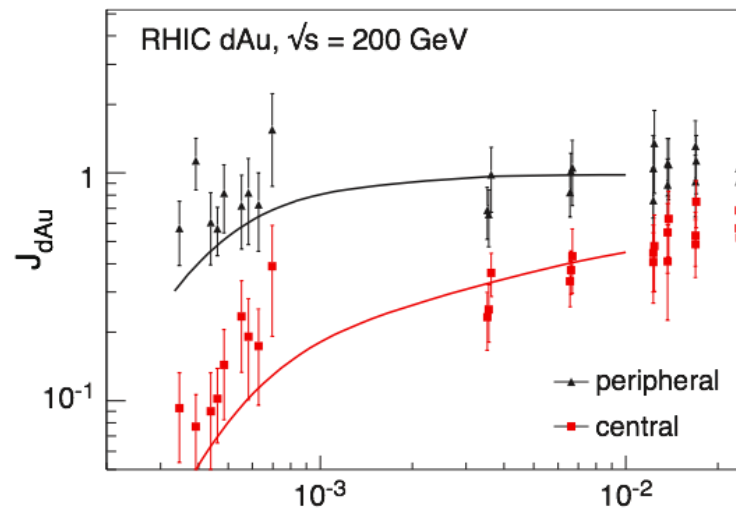
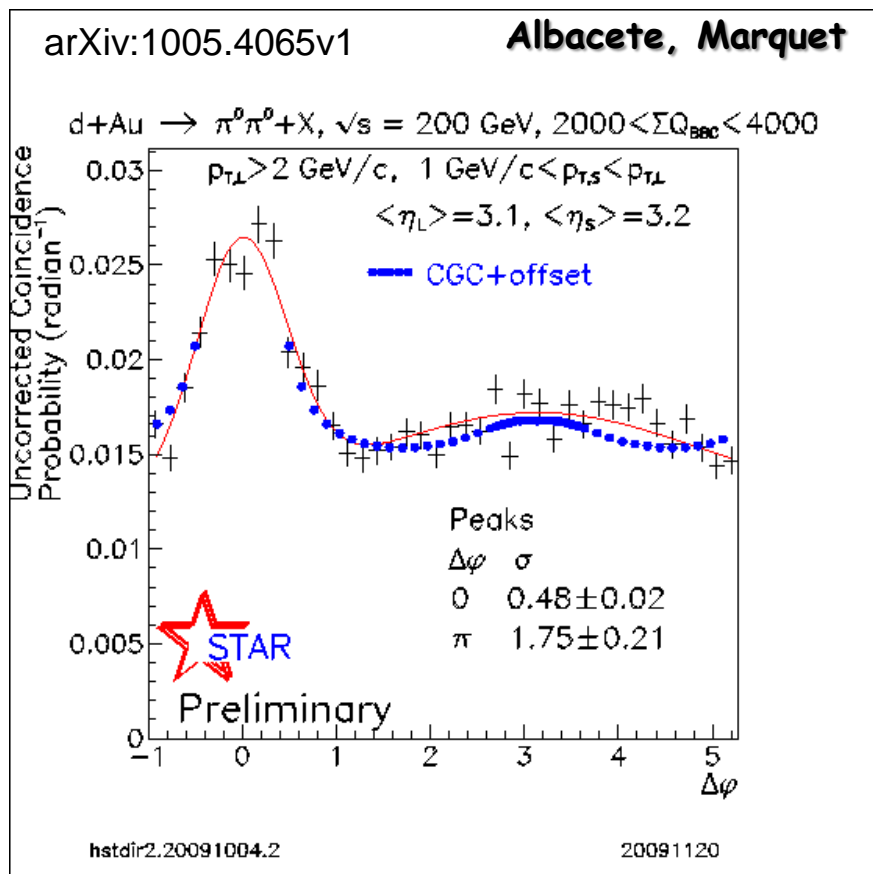
arXiv:1008.3989v1





# Dihadron correlation at RHIC forward dAu program

CGC model

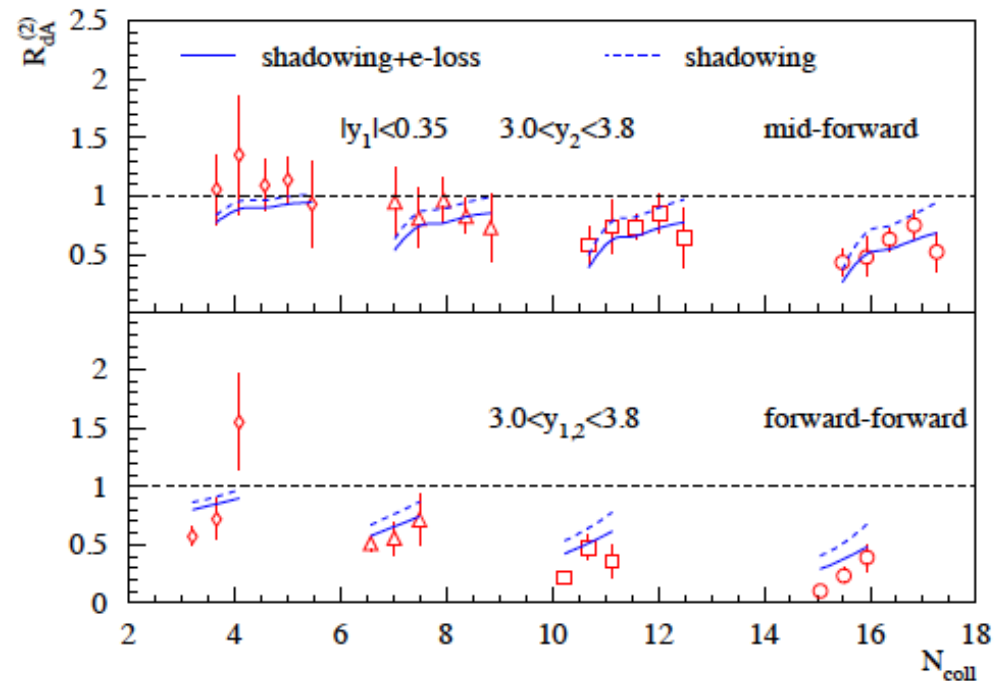
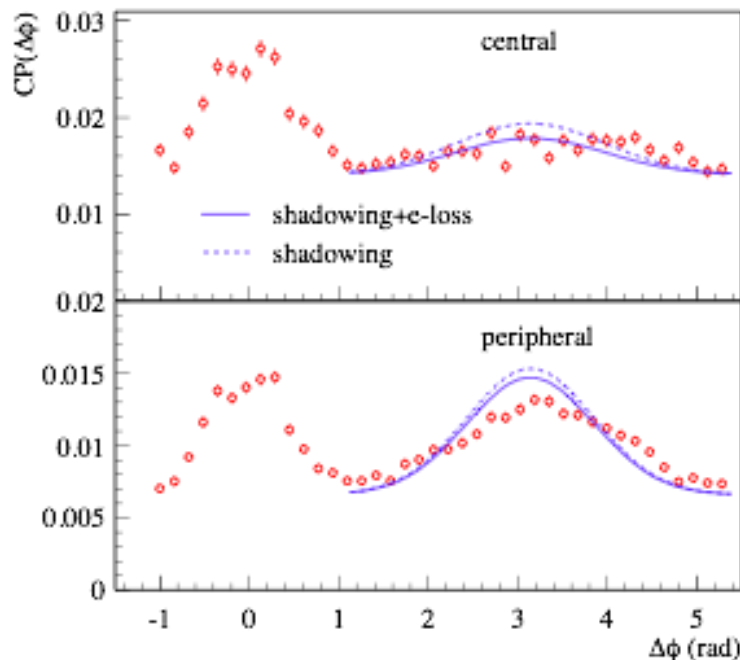


Bowen et al. 2012

# Dihadron correlation at RHIC forward dAu program

Multiple parton interaction  
(Non CGC formalism)

Kang,Vitev,Xing, arXiv:1112.6021v1



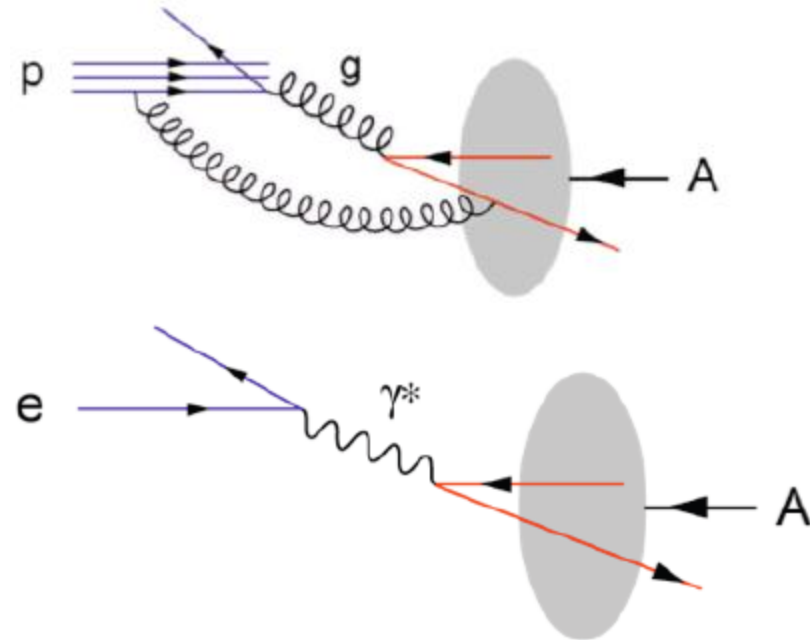
# Dihadron correlation at eRHIC

## EIC:

- Extract the spatial multi-gluon correlations and study their non-linear evolution
- Control final state
  - essential for understanding the transition from a deconfined into a confined state.(in AA)

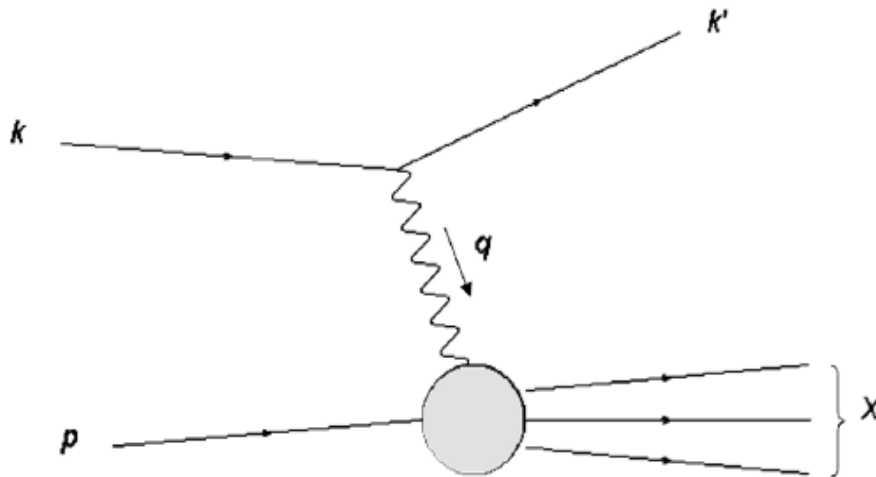
## Advantage over p(d)A:

- eA experimentally much cleaner
  - no “spectator” background to subtract
  - Access to the exact kinematics of the DIS process ( $x$ ,  $Q^2$ )



# DIS kinematics

## Event wise variables:



$$\begin{aligned}
 s &= (p + k)^2, \\
 W^2 &= (p + q)^2, \\
 Q^2 &= -q^2, \\
 x &= \frac{Q^2}{2p \cdot q} = \frac{Q^2}{W^2 + Q^2}, \\
 y &= \frac{p \cdot q}{p \cdot k} = \frac{Q^2}{sx}, \\
 \nu &= p \cdot q / M_p
 \end{aligned}$$

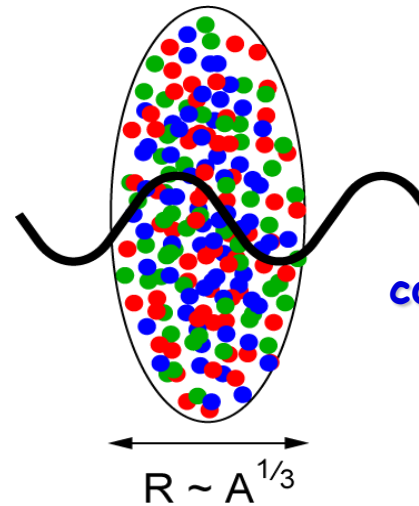
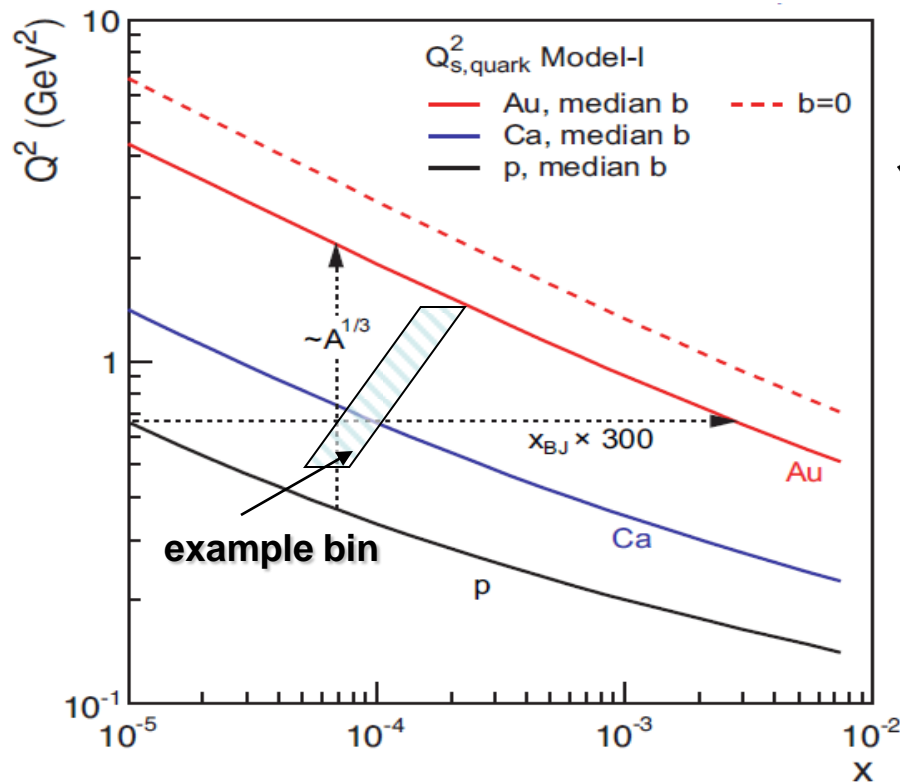
## Particle wise variables:

$p_T$  is defined with respect to virtual photon

$$z_h = \frac{p_h \cdot p}{q \cdot p}$$

# theoretical prediction from CGC

Pocket formula:  $Q_s^2(x) \sim A^{1/3} \left( \frac{1}{x} \right)^\lambda \sim \left( \frac{A}{x} \right)^{1/3}$



$L \sim A^{1/3}$   
 Probe interacts  
 coherently with all nucleons

**Bin:  $0.5 < Q^2 < 1.5 \text{ GeV}^2$ ,  $0.6 < y < 0.8$**

$\langle x \rangle = 1.01 \times 10^{-4}$ ,

$\langle y \rangle = 0.69$ ,

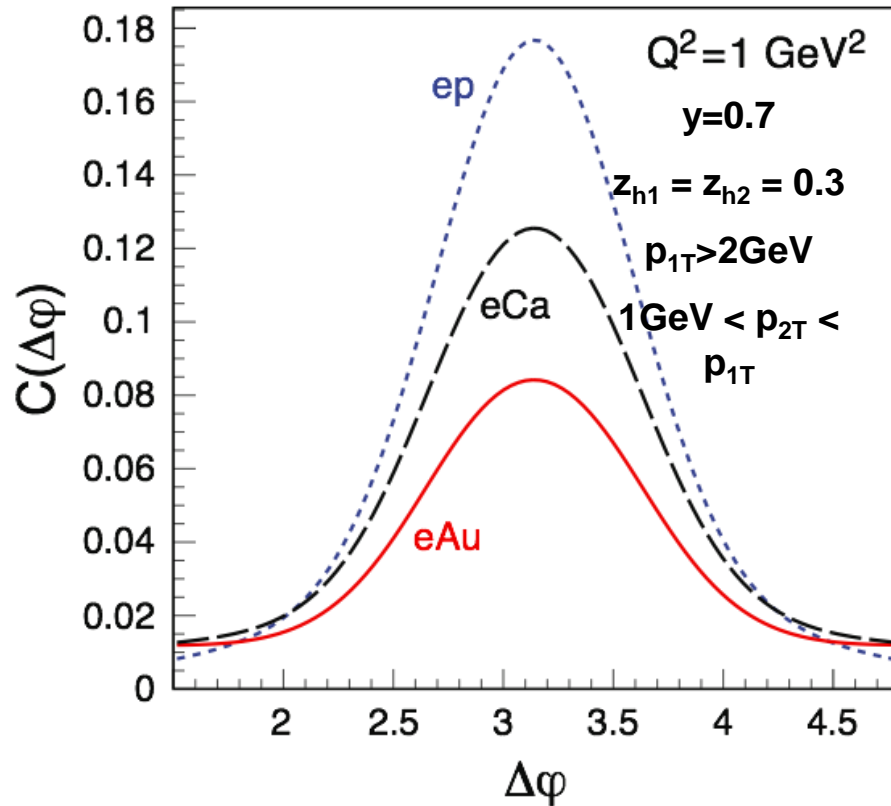
$\langle Q^2 \rangle = 0.84 \text{ GeV}^2$ ,

$\langle W^2 \rangle = 8322 \text{ GeV}^2$ ,

$\langle \nu \rangle = 4434 \text{ GeV}$

# theoretical prediction from CGC

Bowen, Dominguez, Yuan 2011/2012



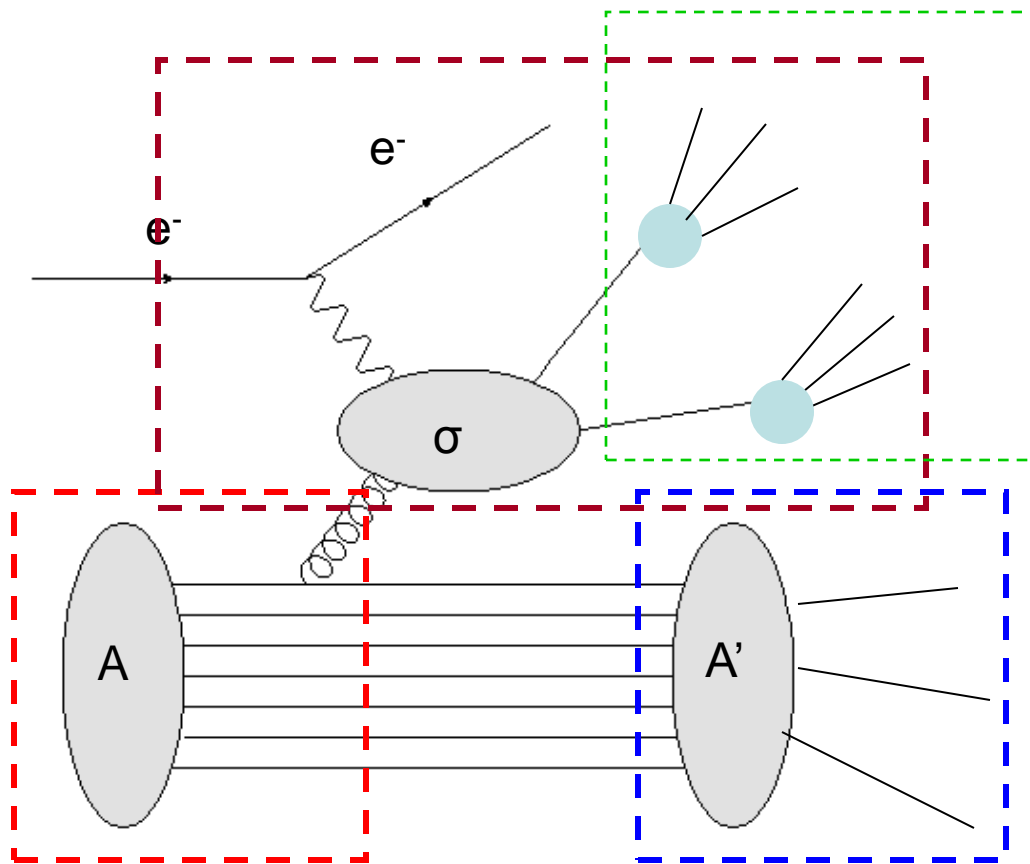
ep:  $Q^2 > Q_s^2$ , dilute system.

eAu:  $Q^2 < Q_s^2$ , dense system.

A factor  $\sim 2$  suppression from  
ep to eAu at EIC energy.

Probing  $x$  range as low as  $10^{-4}$

# Our Monte Carlo approach for the eA simulation



A hybrid model consisting of DPMJet and PYTHIA with nPDF EPS09.

Nuclear geometry by DPMJet and nPDF provided by EPS09.

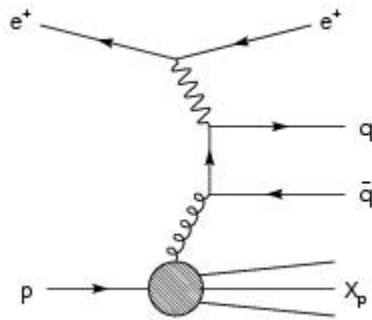
Parton level interaction and jet fragmentation completed in PYTHIA.

Nuclear evaporation ( gamma dexcitation/nuclear fission/fermi break up ) treated by DPMJet

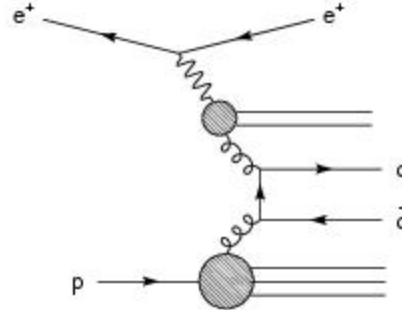
Energy loss effect from routine by Salgado&Wiedemann to simulate the nuclear fragmentation effect in cold nuclear matter (under development).

# Dihadron correlation at eRHIC

PGF

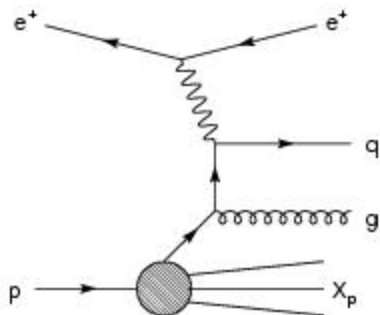


Resolved

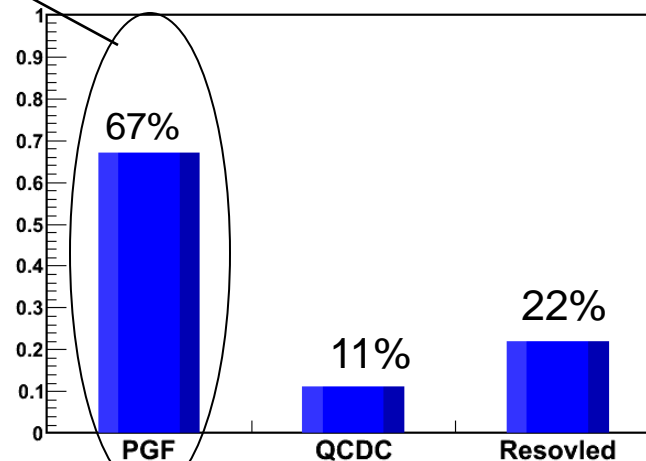


Dominant process:  
Photon Gluon Fusion  
(PGF), sensitive to  
the property of strong  
gluon field.

QCDC



Process fraction in dihadron correlatin

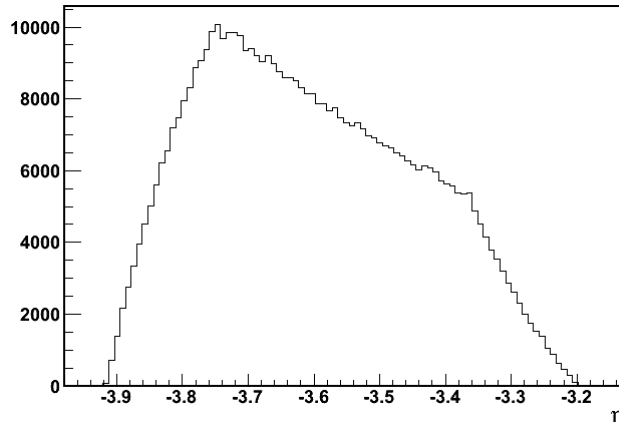


$Q^2=4\text{GeV}^2$   
from PYTHIA  
simulation

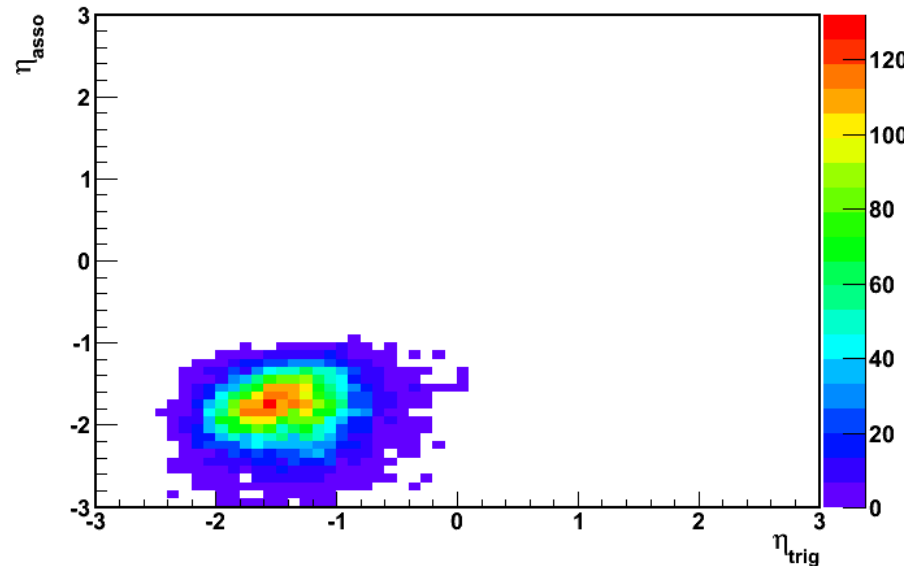


# Results for $Q^2=1 \text{ GeV}^2$

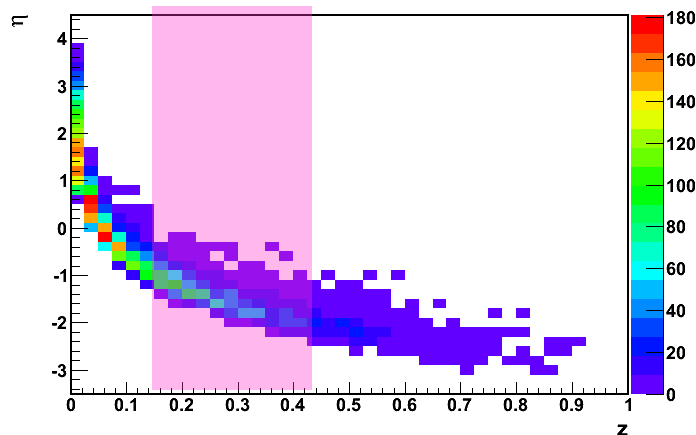
Scattered electron pseudo-rapidity



$\eta$  correlation



Leading particle span



Trigger/associate particle cut:

$$|\eta| < 4 \quad (2 < \theta < 178 \text{ deg}),$$

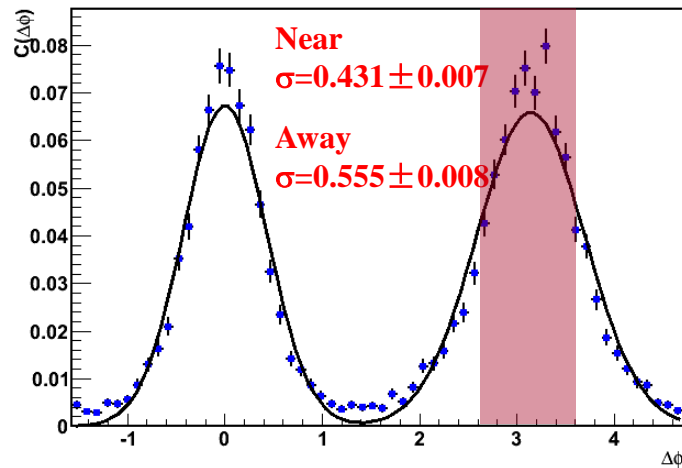
$$p_{\text{T}}^{\text{Trig}} > 2, \quad 1 < p_{\text{T}}^{\text{Asso}} < 2$$

$$0.15 < z^{\text{Trig,Asso}} < 0.45$$

# Results for $Q^2=1 \text{ GeV}^2$

$\Delta\phi$  distribution

ep



30+100 GeV 10M events

$0.5 < Q^2 < 1.5$ ,  $0.6 < y < 0.8$

$|\eta| < 4$  ( $2 < \theta < 178$  deg),

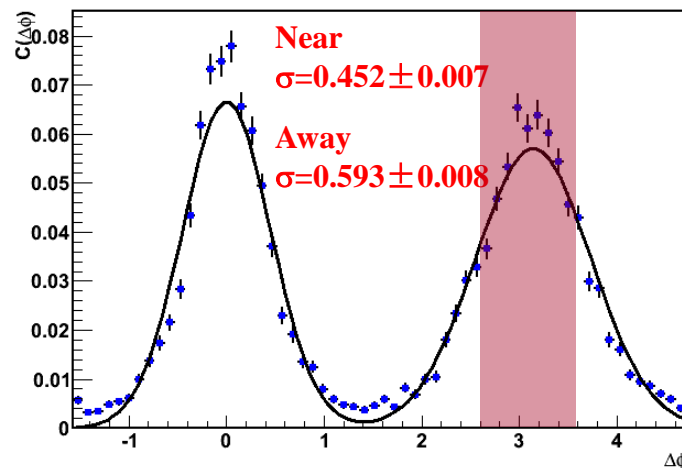
$p_T^{\text{Trig}} > 2$ ,  $1 < p_T^{\text{Asso}} < 2$

$0.15 < z^{\text{Trig,Asso}} < 0.45$

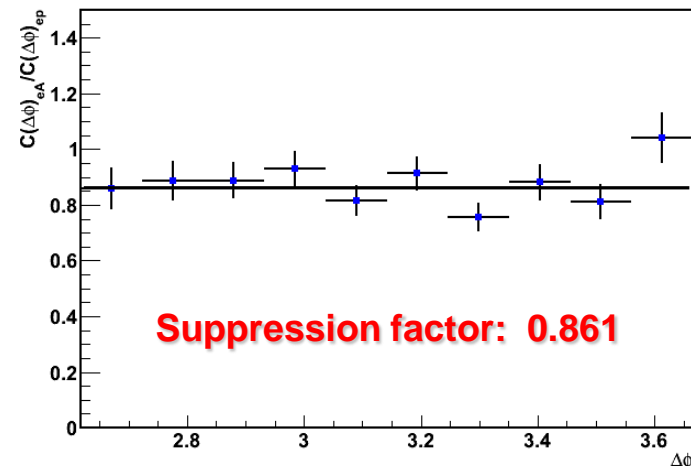
**Nuclear PDF gives no strong suppression effect**

$\Delta\phi$  distribution

eAu

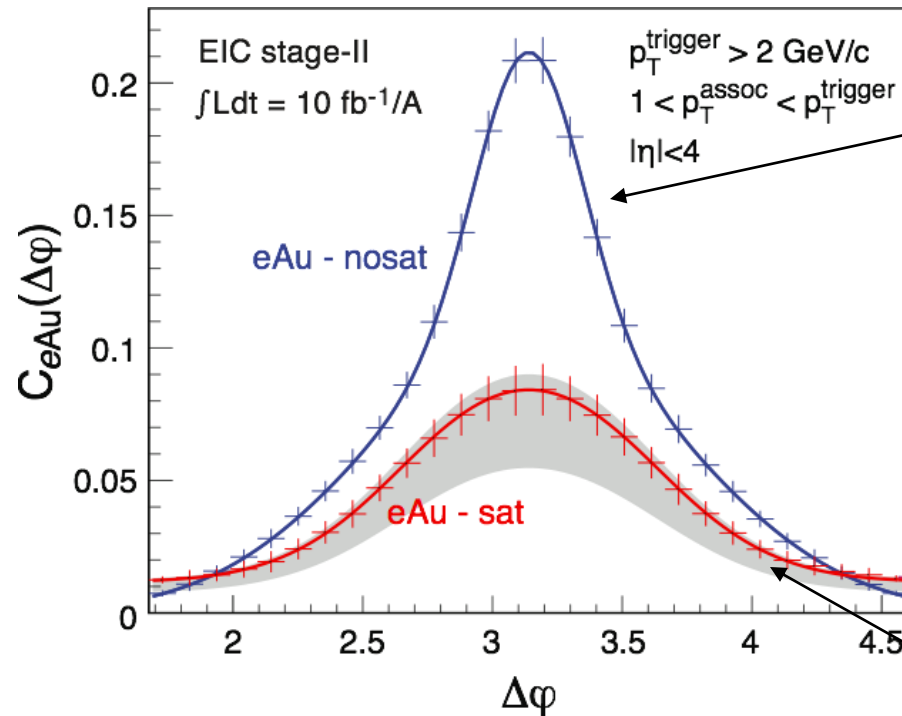


Ratio



# Compare with CGC prediction

EIC white paper

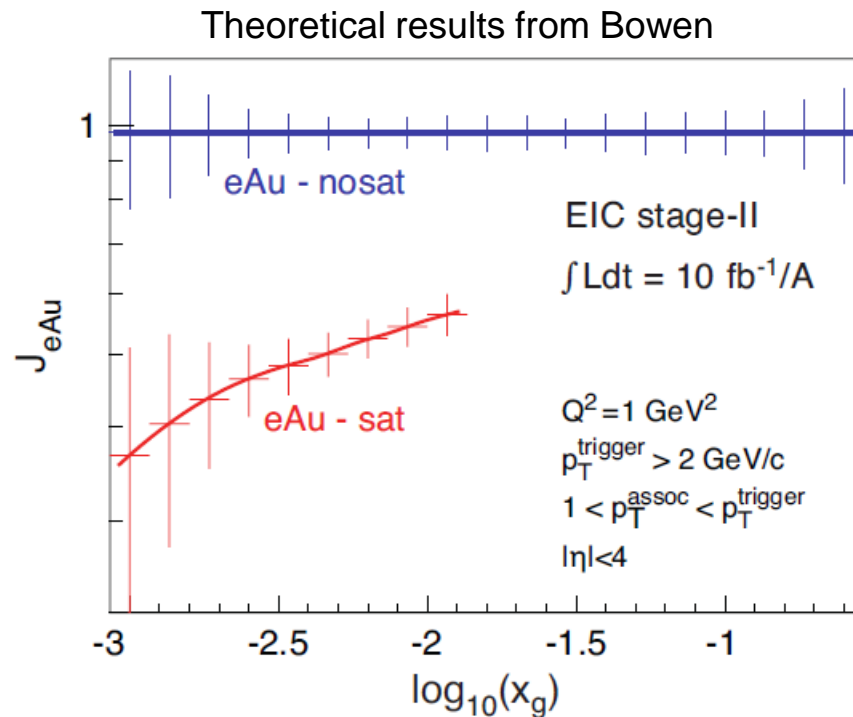


**Results from our Monte Carlo, no saturation included.**

**A good discrimination of different models with a few months running.**

**Prediction from CGC calculation.**

# Compare with CGC prediction



Similar to  $J_{dA}$  we can define a  $J_{eA}$  here.

$$J_{eA} = \frac{1}{A^{1/3}} \frac{\sigma_{eA}^{\text{pair}} / \sigma_{eA}}{\sigma_{ep}^{\text{pair}} / \sigma_{ep}}$$

The absence of nuclear effect would correspond to  $J_{eA}=1$ .

$J_{eA} < 1$  would signify suppression of dihadron correlation.

Well controlled kinematics, pronounced signal between sat and non-sat.

# The power of Monte Carlo

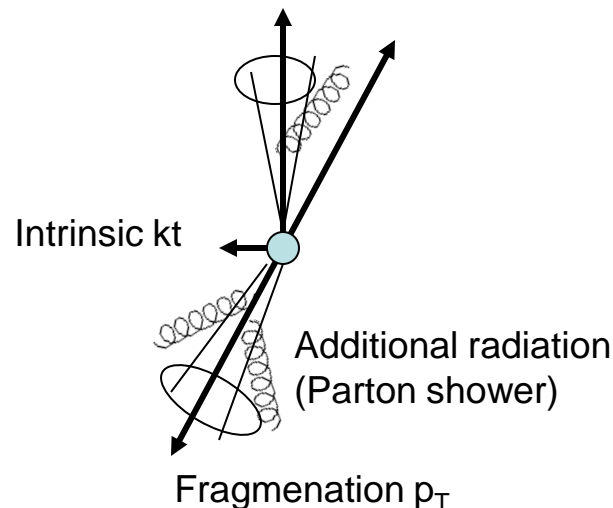
**2 → 2 back to back parton**

**Intrinsic  $k_T$  smears parton back to back correlation**

**Fragmentation  $p_T$  introduce  $p_T$  with respect to jet axis for hadrons.**

**Parton shower affects the parton  $p_T$  imbalance and the jet profile.**

**Medium energy loss effect**



ep 30x100GeV	MC approach	Theoretical model
Intrinsic $k_T$	PARP(91)=0.4	$0.4 < Q_s^2 < 0.6 \text{ GeV}^2$
Fragmentation $p_T$	PARJ(21)=0.4	$\langle p_T^2 \rangle = 0.2 \text{ GeV}^2$
Parton shower	IS/FS	Not available

# The power of Monte Carlo

With only intrinsic  $k_T$ , no fragmentation  
pt, no Parton Shower

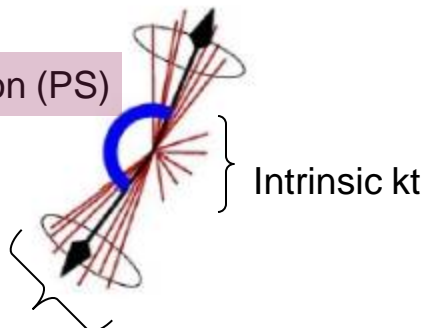
MC side

Theory side

Intrinsic  $k_T = 0.4 \text{ GeV}$

$0.4 < Q_s^2 < 0.6 \text{ GeV}^2$

Additional radiation (PS)



Fragmentation pt

ep 30x100GeV

**MC cuts:**

$3.5 < Q^2 < 4.5$

$0.65 < y < 0.75$

$p_T \text{ trig} > 2 \text{ GeV}$

$1 < p_T \text{ asso} < p_T \text{ trig}$

$0.25 < z_1, z_2 < 0.35$

**Theoretical input:**

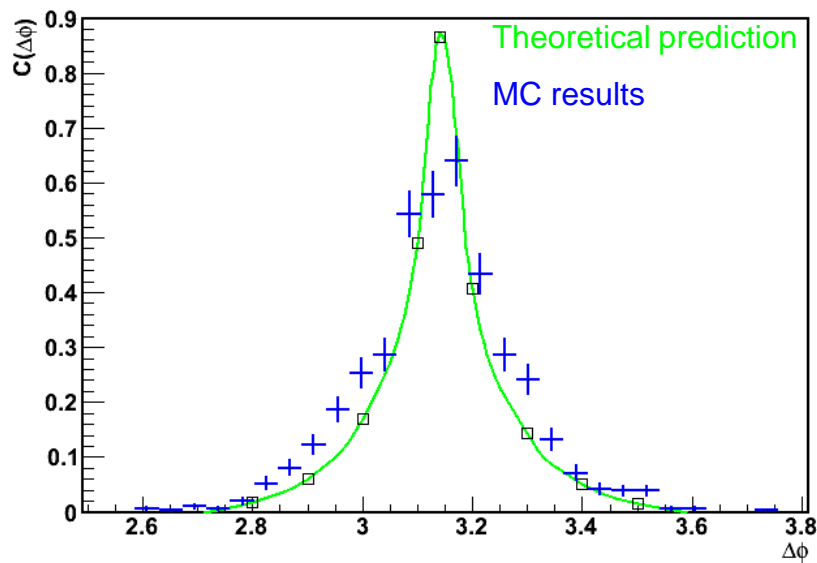
$Q^2 = 4$

$y = 0.7$

$p_T \text{ trig} > 2 \text{ GeV}$

$1 < p_T \text{ asso} < p_T \text{ trig}$

$z_1 = z_2 = 0.3$



Theoretical curves from B.W.Xiao

7/31/2012

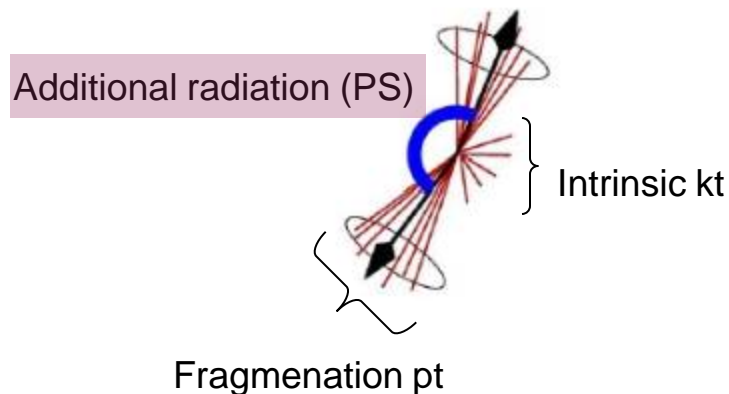
RBRC Forward physics  
workshop

22

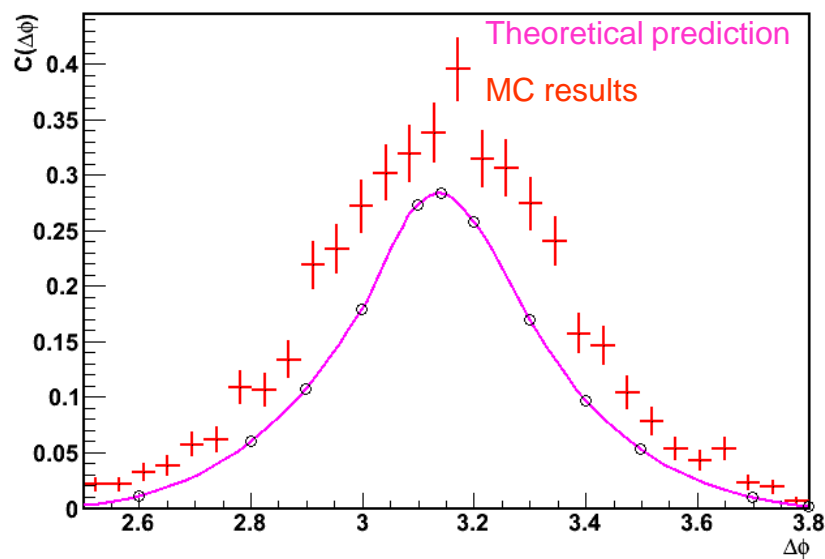
# The power of Monte Carlo

Intrinsic  $k_T$  + fragmentation  $p_T$ , no Parton Shower

MC side	Theory side
Intrinsic $k_T = 0.4 \text{ GeV}$ Frag $p_T = 0.4 \text{ GeV}$	$0.4 < Qs^2 < 0.6 \text{ GeV}^2$ $\langle p_T^2 \rangle = 0.2 \text{ GeV}^2$

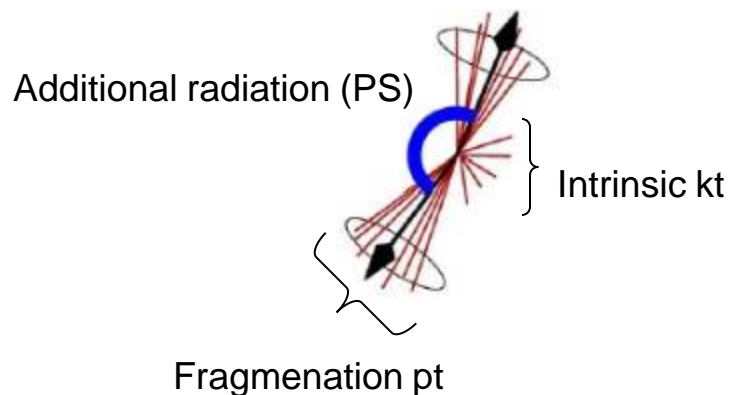


Seeing the fact that we have different treatment to PDF and fragmentation process, we have come to an agreement in ep for these two approaches.



Theoretical curves from B.W.Xiao

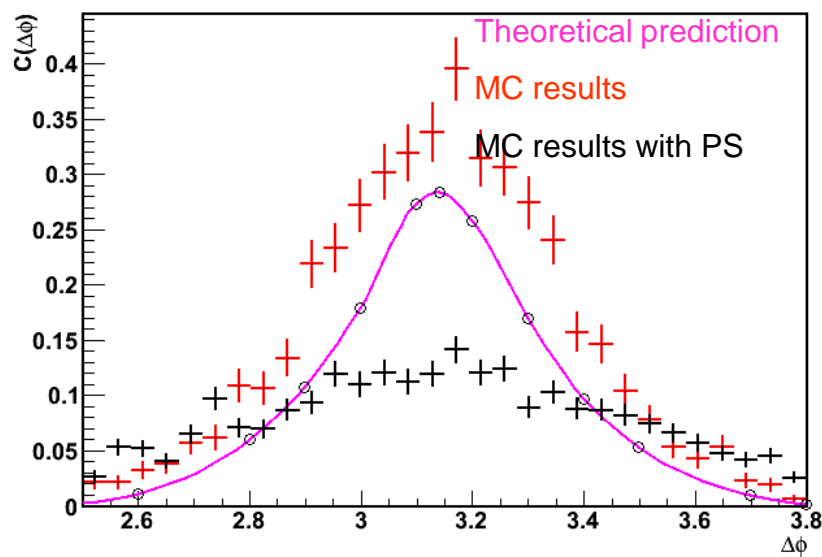
# The power of Monte Carlo



As parton shower in MC can be used as a good way to compensate the theory results.  
Stretch the theoretical curve of eAu based on the PS effect on ep.

Intrinsic  $k_t$  + fragmentation  $p_t$ , with Parton Shower on

MC side	Theory side
<b>Intrinsic <math>k_T = 0.4 \text{ GeV}</math></b>	<b><math>0.4 &lt; Qs^2 &lt; 0.6 \text{ GeV}^2</math></b>
<b>Frag <math>p_T = 0.4 \text{ GeV}</math></b>	<b><math>\langle p_T^2 \rangle = 0.2 \text{ GeV}^2</math></b>
<b>Parton shower on</b>	



Theoretical curves from B.W.Xiao



# Energy loss effect under development

Possible to include some final energy loss effect.

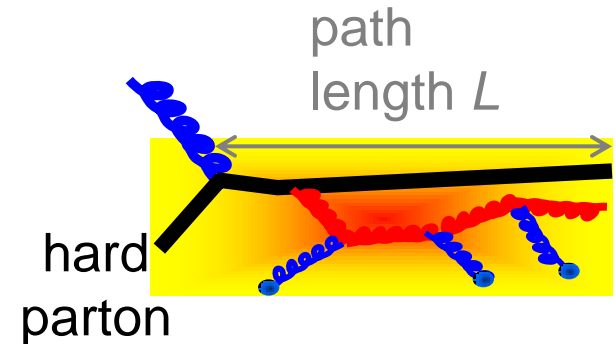
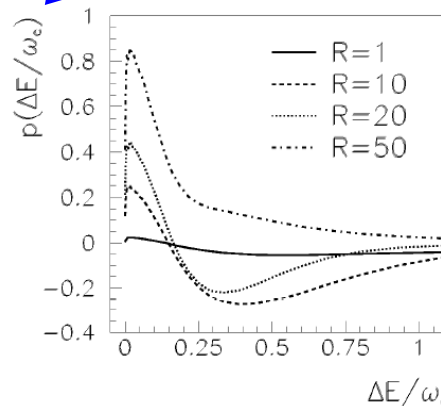
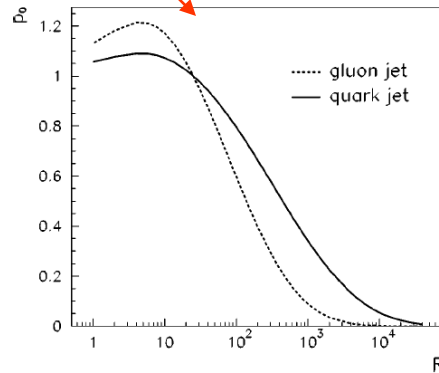
According to PyQM developed by Raphael.

The probability for a parton to loose energy  $\Delta E$  is given by

$$P(\Delta E) = \sum_{n=0}^{\infty} \frac{1}{n!} \left[ \prod_{i=1}^n \int d\omega_i \frac{dI(\omega_i)}{d\omega} \right] \times \left( \Delta E - \sum_{i=1}^n \omega_i \right) \exp \left[ - \int d\omega \frac{dI}{d\omega} \right]$$

Salgado & Wiedemann PRD 68, 014008 (2003)

$$= p_0 \delta(\Delta E) + p(\Delta E)$$



This radiation spectrum usually depends on the length of medium  $L$ , and the transport coefficient

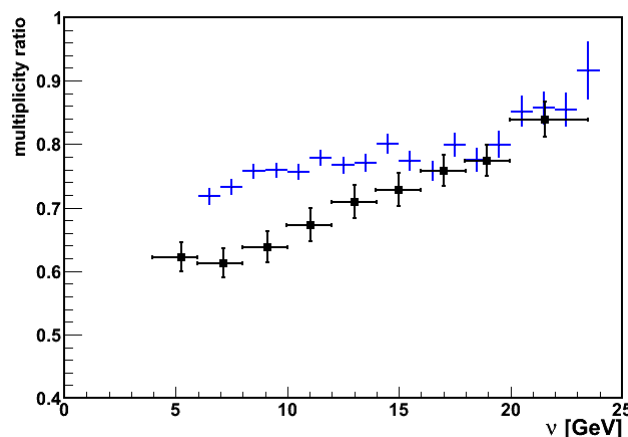
$$\hat{q} = \langle k_t^2 \rangle_{\text{medium}} / \lambda$$

# Energy loss effect under development

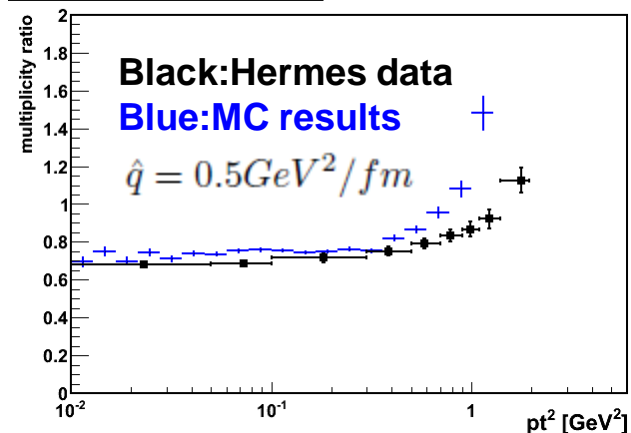
Comparison with Hermes data  
27.6 GeV eXe vs eD

$$R_A^h(Q^2, \nu, z_h, P_\perp^2) = \frac{N_A^h(Q^2, \nu, z_h, P_\perp^2) / N_A^e(Q^2, \nu)}{N_D^h(Q^2, \nu, z_h, P_\perp^2) / N_D^e(Q^2, \nu)}$$

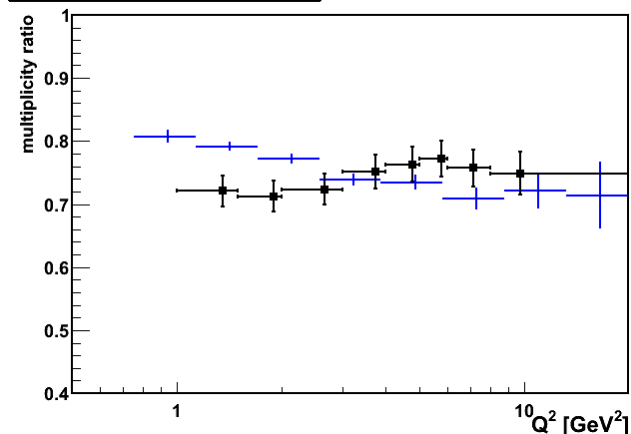
multiplicity ratio vs  $\nu$  for  $\pi^+$



multiplicity ratio vs  $pt^2$  for  $\pi^+$



multiplicity ratio vs  $Q^2$  for  $\pi^+$



# Summary & Prospects

- Dihadron correlation is a very important measurement in the future eRHIC eA program.
- A generic Monte Carlo generator design based on pQCD calculation in the vacuum with flexible nuclear effects added on.
- Energy loss effect in cold nuclear medium to be included in this Monte Carlo.
- Can be utilized to understand dA or pA data and extract the model parameters as an input in our eAu simulation.

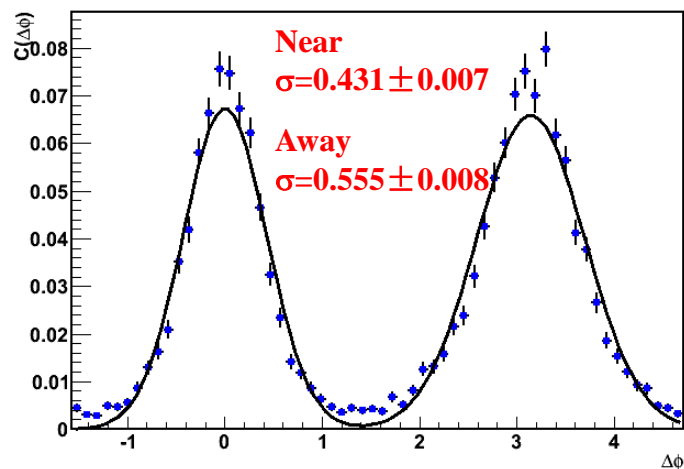
Thank you for your attention

Backup slides

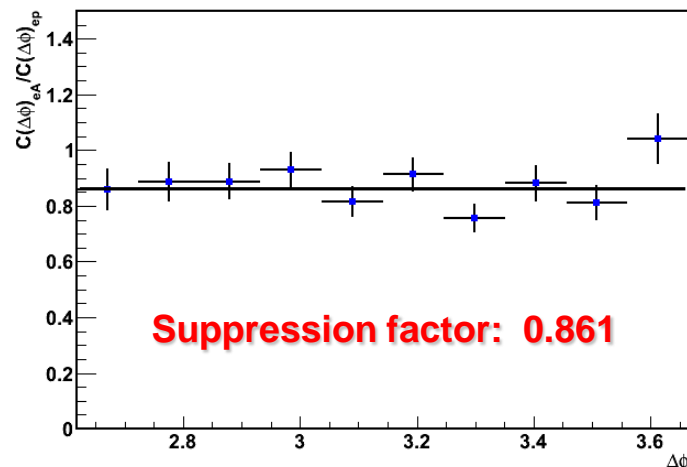
# Results $Q^2=1 \text{ GeV}^2$

$\Delta\phi$  distribution

ep

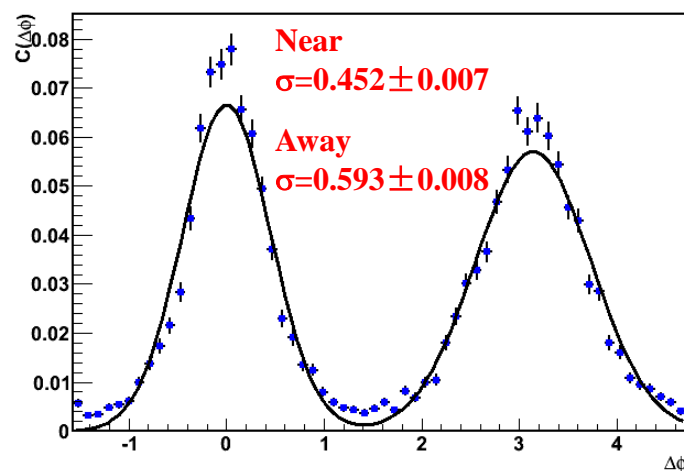


Ratio



$\Delta\phi$  distribution

eAu



30+100GeV 10M events

Total cross section(ep):34.95nb

Integrated Luminosity(ep):0.286fb<sup>-1</sup>

$0.5 < Q^2 < 1.5$ ,  $0.6 < y < 0.8$

$|\eta| < 5$  (  $0.772 < \theta < 179.228$  ),

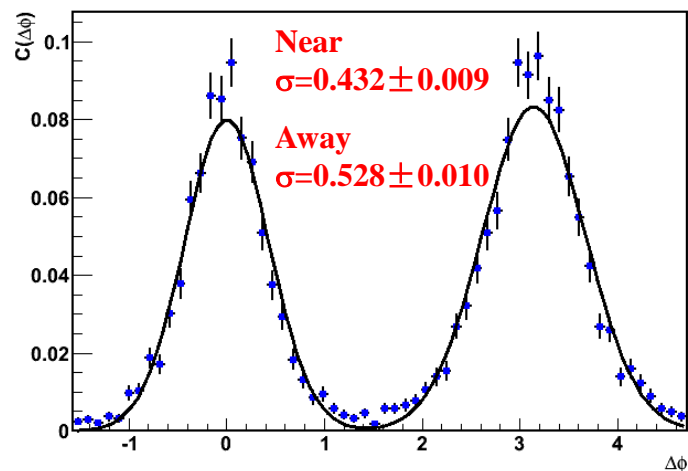
$p_t^{\text{Trig}} > 2$ ,  $1 < p_t^{\text{Asso}} < 2$

$0.1 < z_{\text{Trig,Asso}} < 0.3$

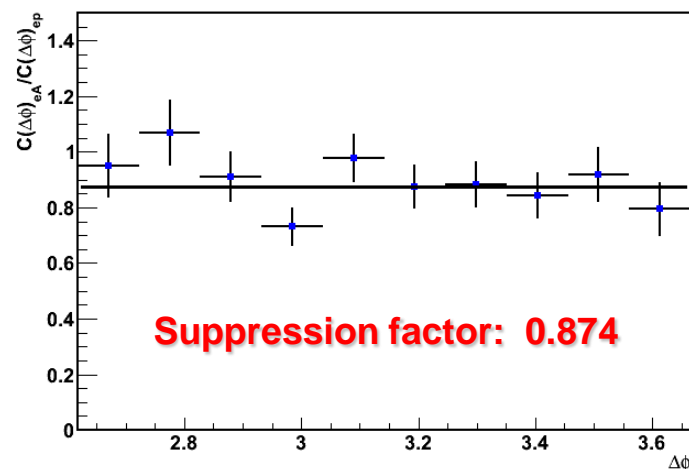
# Results $Q^2=4 \text{ GeV}^2$

$\Delta\phi$  distribution

ep

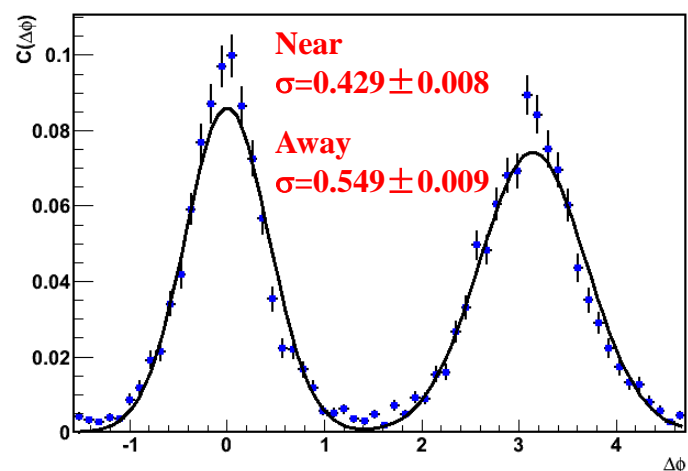


Ratio



$\Delta\phi$  distribution

eAu



30+100GeV 2M events

Total cross section(ep):2.3nb

Integrated Luminosity(ep):0.87fb<sup>-1</sup>

$3.5 < Q^2 < 4.5$ ,  $0.6 < y < 0.8$

$|\eta| < 5$  (  $0.772 < \theta < 179.228$  ),

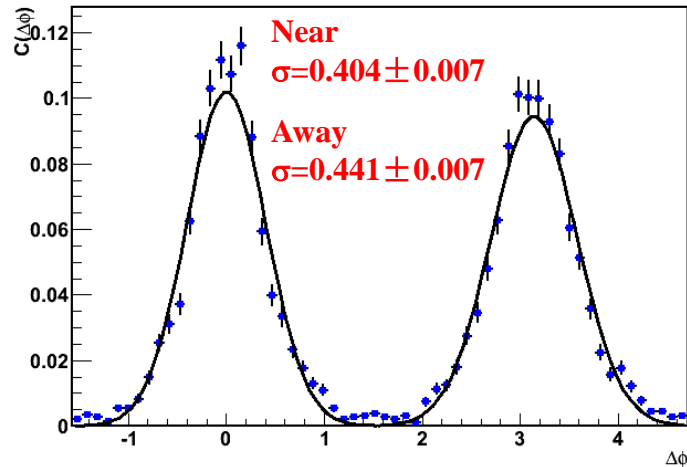
$p_t^{\text{Trig}} > 2$ ,  $1 < p_t^{\text{Asso}} < 2$

$0.1 < z_{\text{Trig,Asso}} < 0.3$

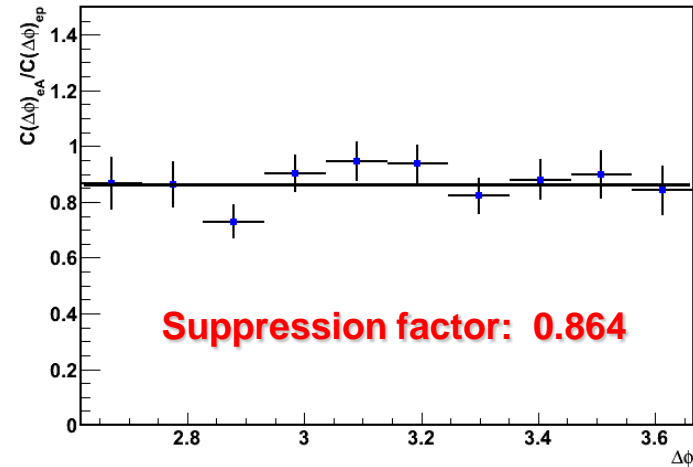
# Results $Q^2=10 \text{ GeV}^2$

$\Delta\phi$  distribution

ep

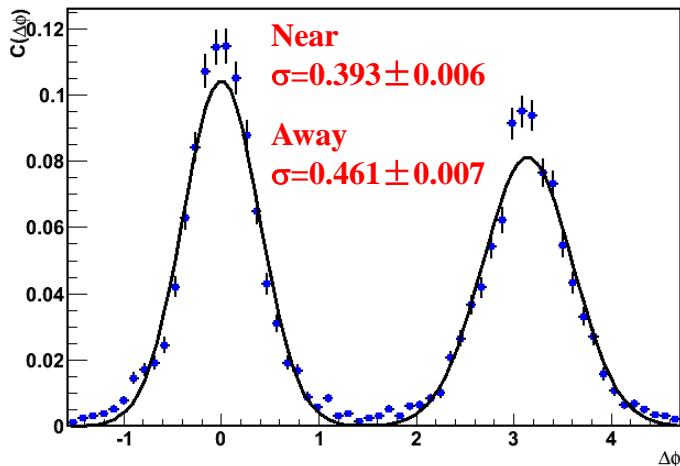


Ratio



$\Delta\phi$  distribution

eAu



30+100GeV 2M events

Total cross section(ep):0.414nb

Integrated Luminosity(ep):4.83fb<sup>-1</sup>

$9.5 < Q^2 < 10.5$ ,  $0.6 < y < 0.8$

$|\eta| < 5$  (  $0.772 < \theta < 179.228$  ),

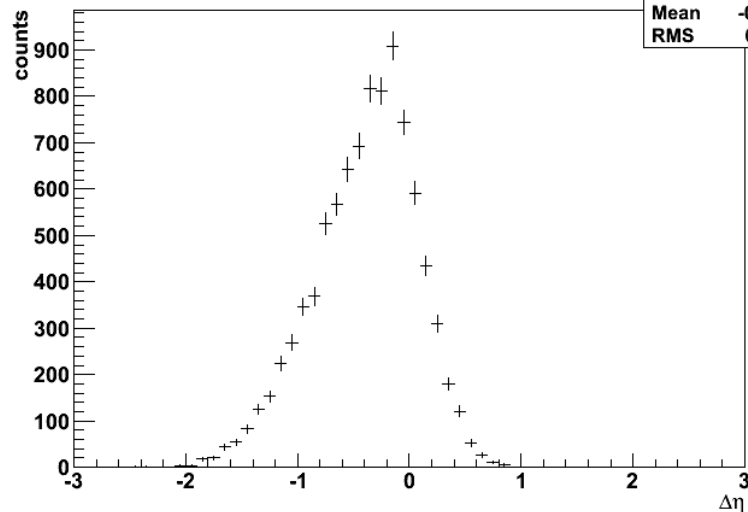
$p_t^{\text{Trig}} > 2$ ,  $1 < p_t^{\text{Asso}} < 2$

$0.1 < z_{\text{Trig,Asso}} < 0.3$

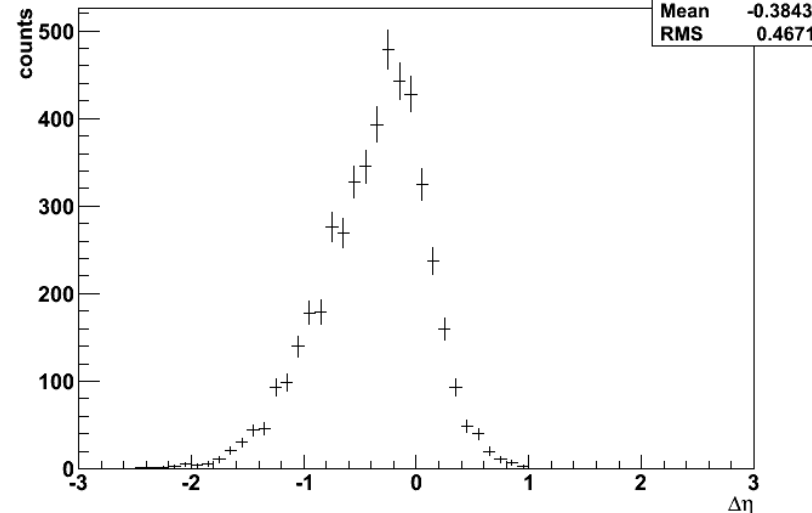


	ep			eAu			eA/ep
	Trig frac Total/accpt	$\sigma(\text{Near})$	$\sigma(\text{Away})$	Trig frac Total/accpt	$\sigma(\text{Near})$	$\sigma(\text{Away})$	ratio
Q2=1	0.538%	$0.431 \pm 0.007$	$0.555 \pm 0.008$	0.706%	$0.452 \pm 0.007$	$0.593 \pm 0.008$	$0.861 \pm 0.043$
Q2=4	1.176%	$0.432 \pm 0.009$	$0.528 \pm 0.010$	1.503%	$0.429 \pm 0.008$	$0.549 \pm 0.009$	$0.874 \pm 0.026$
Q2=10	1.619%	$0.404 \pm 0.007$	$0.441 \pm 0.007$	1.958%	$0.393 \pm 0.006$	$0.461 \pm 0.007$	$0.864 \pm 0.024$

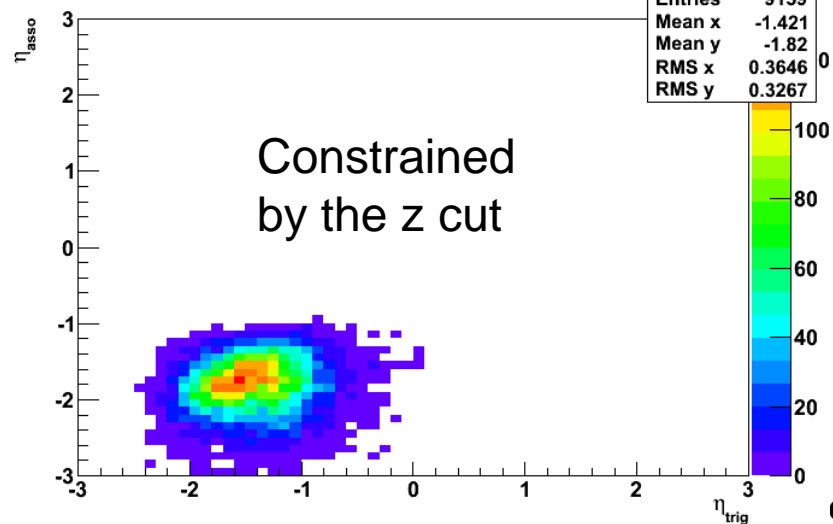
Q2=1 unsmeared

 $\Delta\eta$  distribution

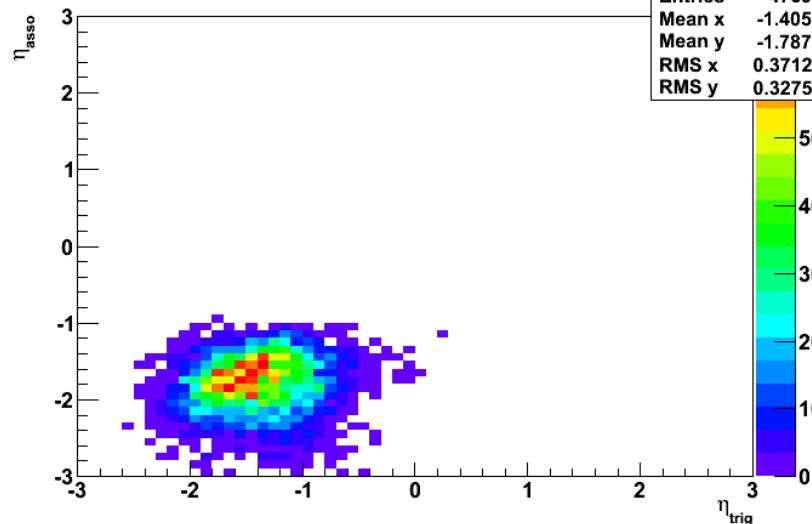
Q2=4 unsmeared

 $\Delta\eta$  distribution

Q2=1 unsmeared

 $\eta$  correlation

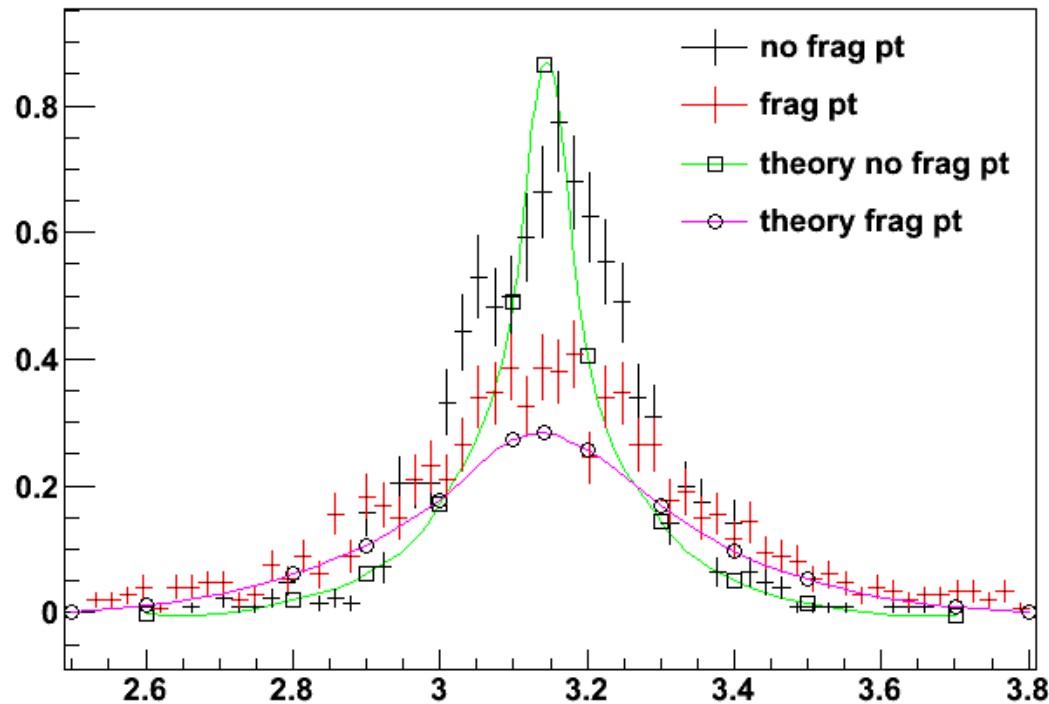
Q2=4 unsmeared

 $\eta$  correlation

**MC cuts:**

Pi0  $3.5 < Q^2 < 4.5$   $0.65 < y < 0.75$

Pt trig  $> 2\text{GeV}$   $1\text{GeV} < \text{Pt asso} < \text{Pt trig}$   $0.25 < z_1, z_2 < 0.35$



Parton shower must be switched off and a reasonable intrinsic  $k_t$  is necessary for this reproduction of ep correlation function.

e+p/A(30+100)

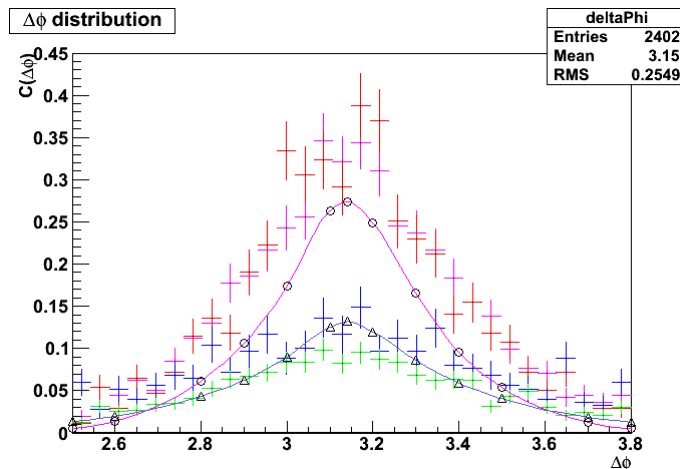
MC cuts:

$\pi^0$

$3.5 < Q^2 < 4.5, 0.65 < y < 0.75$

$p_{t1} > 2 \text{ GeV}, 1 \text{ GeV} < p_{t2} < p_{t1}$

$0.25 < z < 0.35$

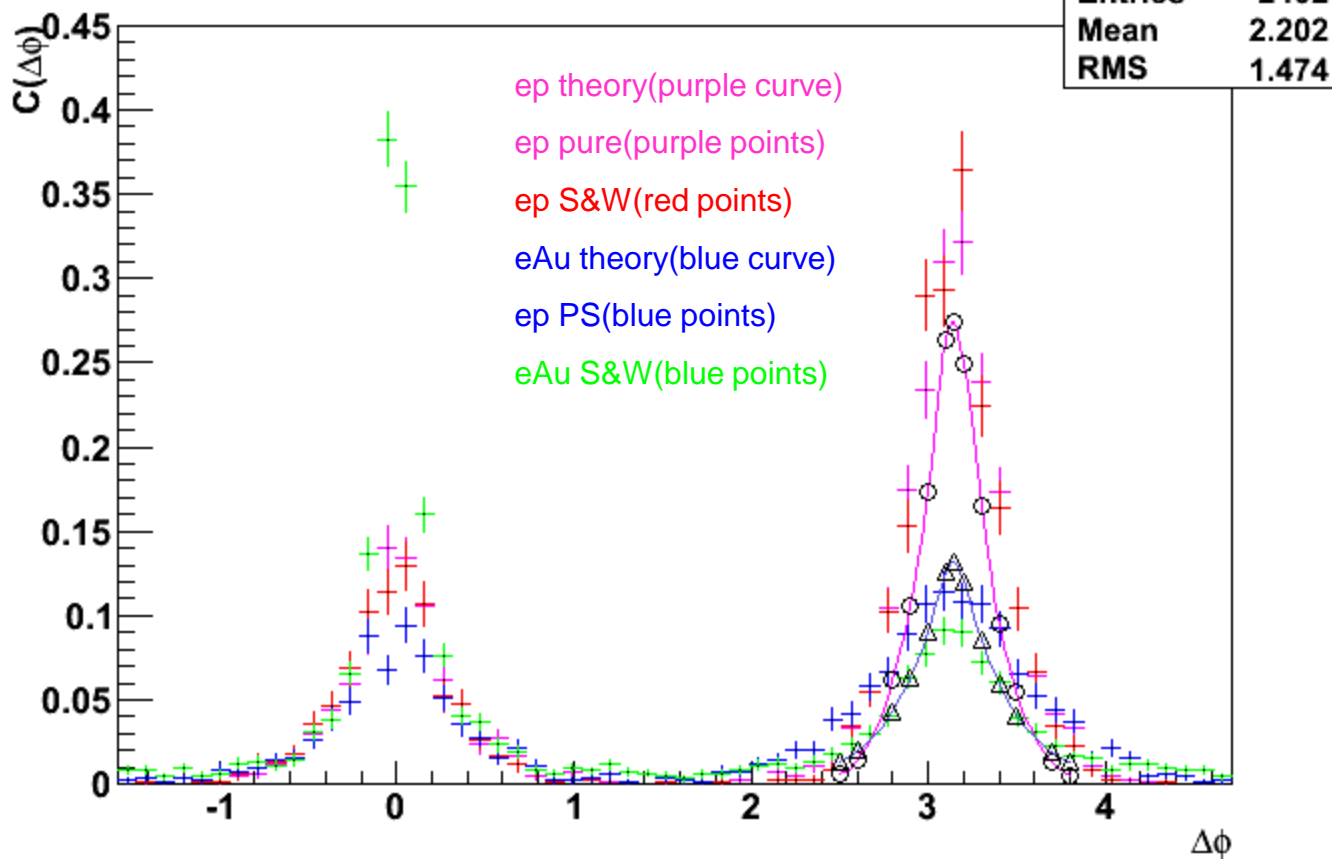


$e\text{Au}(\text{S\&W})/e\text{p}(\text{S\&W})=0.27$

$e\text{Au}(\text{S\&W})/e\text{p}(\text{PS})=0.76$

$e\text{Au}(\text{theory})/e\text{p}(\text{theory})=0.48$

$\Delta\phi$  distribution



Q2=1

Process fraction in current Bin:

LODIS:52.7% PGF:5% QCDC:1.66%

DIFF:12.8% Resovled:21.26%

Contribution to dihadron:

PGF:54.45% QCDC:7.75%

Resovled:37.42%

Q2=4

Process fraction in current Bin:

LODIS:67.44% PGF:7.43% QCDC:2.06%

DIFF:8.35% Resovled:10.61%

Contribution to dihadron:

PGF:66.22% QCDC:11.09%

Resovled:22.42%

Q2=10

Process fraction in current Bin:

LODIS:80.87% PGF:4.88% QCDC:1.54%

DIFF:4.98% Resovled:5.43%

Contribution to dihadron:

PGF:68.63% QCDC:15.18%

Resovled:13.08%

# The power of Monte Carlo

## Jetset fragmentation

### MC cuts:

$3.5 < Q_2 < 4.5$

$0.65 < y < 0.75$

$p_{t \text{ trig}} > 2 \text{ GeV}$

$1 < p_{t \text{ asso}} < p_{t \text{ trig}}$

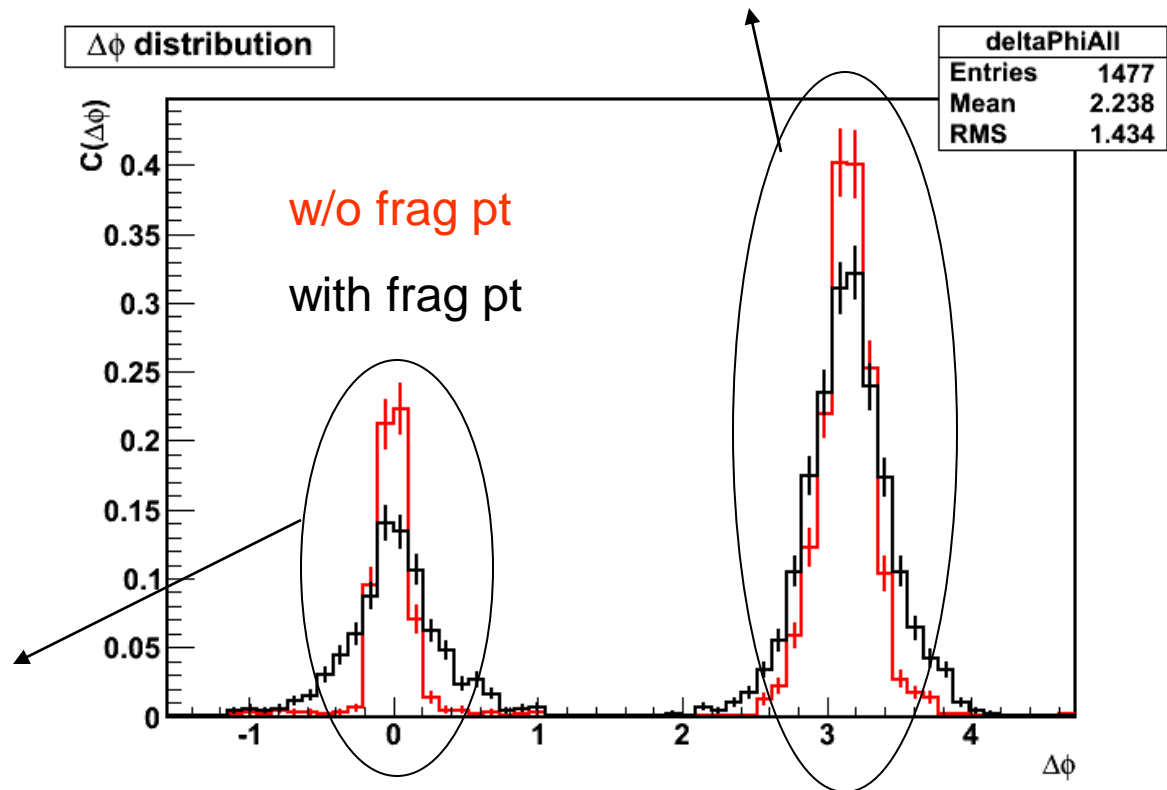
$0.25 < z_1, z_2 < 0.35$

Intrinsic  $k_t = 0.7$

Fragmentation  $p_t = 0.4$

Near side mostly  
affected by the  
fragmentation  $p_t$ .

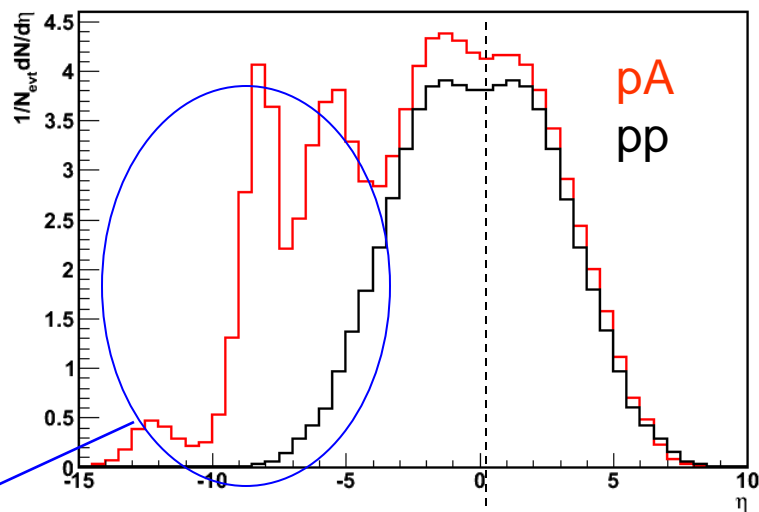
Away side dominated by the intrinsic  $k_t$



# Possible application in pA

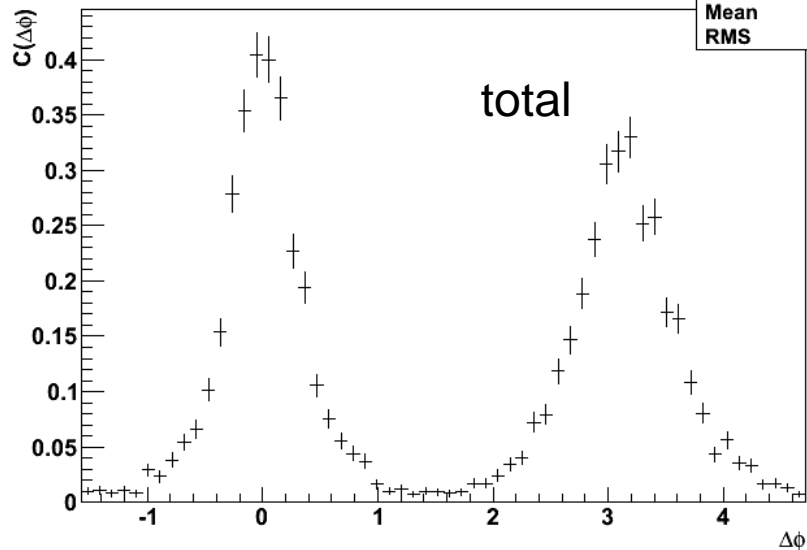
Extending to the pA collision.  
Replace the PDF in PYTHIA for the  
nucleus beam, nuclear break up  
add on.

pA Ncoll=1 compared to pp



Nucleus remnant region,  
Structure from nuclear break up.

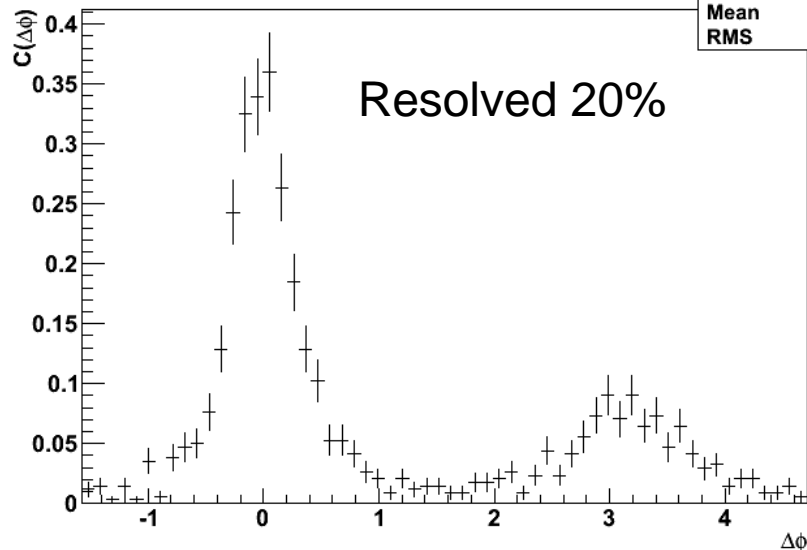
$\Delta\phi$  distribution



deltaPhi	
Entries	6299
Mean	1.593
RMS	1.635

total

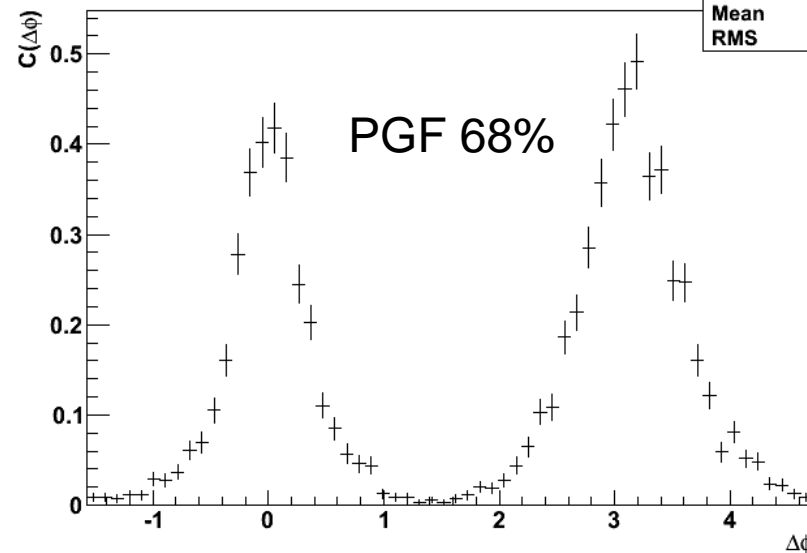
$\Delta\phi$  distribution



deltaPhi	
Entries	1265
Mean	0.9089
RMS	1.503

Resolved 20%

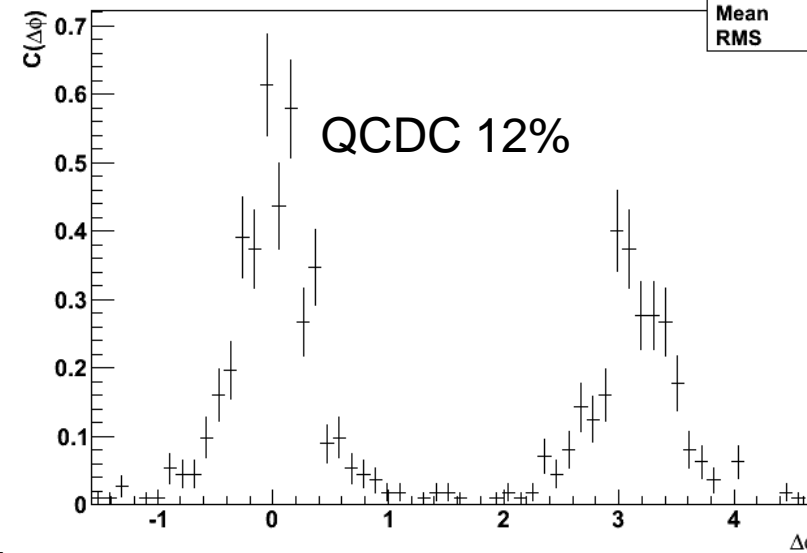
$\Delta\phi$  distribution



deltaPhi	
Entries	4271
Mean	1.856
RMS	1.612

PGF 68%

$\Delta\phi$  distribution



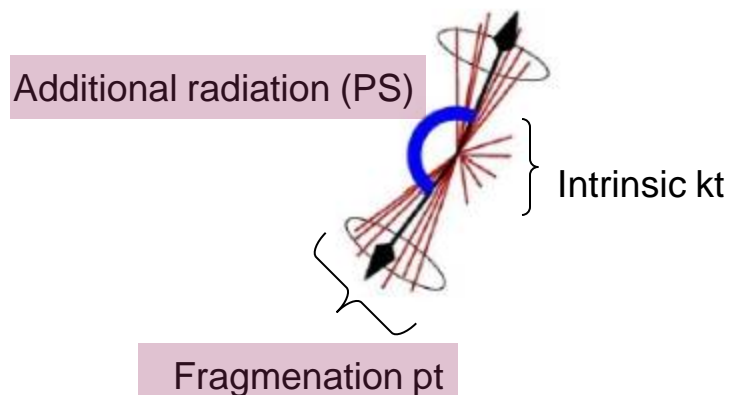
deltaPhi	
Entries	763
Mean	1.255
RMS	1.581

QCDC 12%



# The power of Monte Carlo

3 factors matter a lot in the decorrelation of back to back jets.



## MC cuts:

$$3.5 < Q^2 < 4.5$$

$$0.65 < y < 0.75$$

$$p_{t \text{ trig}} > 2 \text{ GeV}$$

$$1 < p_{t \text{ asso}} < p_{t \text{ trig}}$$

$$0.25 < z_1, z_2 < 0.35$$

$$\text{PARP}(91) = 0.7$$

$$\text{PARJ}(21) = 0.$$

7/31/2012

## Theoretical cuts:

$$Q^2 = 4$$

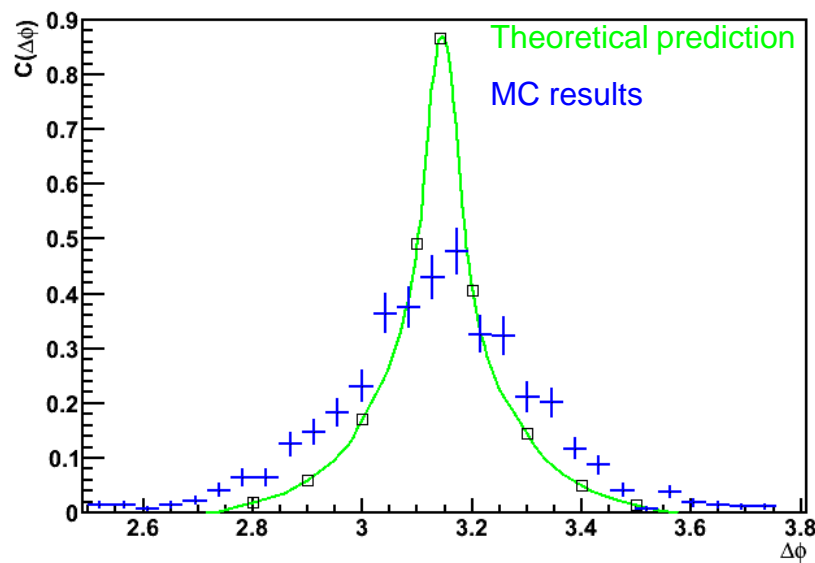
$$y = 0.7$$

$$p_{t \text{ trig}} > 2 \text{ GeV}$$

$$1 < p_{t \text{ asso}} < p_{t \text{ trig}}$$

$$z_1 = z_2 = 0.3$$

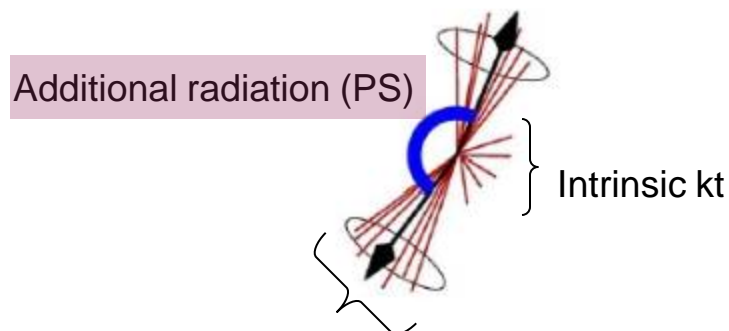
Intrinsic  $k_t = 0.7 \text{ GeV} \sim 0.4 < Q_s^2 < 0.6 \text{ GeV}^2$  in the model  
No fragmentation pt.



Theoretical curves from B.W.Xiao

# The power of Monte Carlo

3 factors matter a lot in the decorrelation of back to back jets.



Fragmentation pt

## MC cuts:

$$3.5 < Q^2 < 4.5$$

$$0.65 < y < 0.75$$

$$p_{t \text{ trig}} > 2 \text{ GeV}$$

$$1 < p_{t \text{ asso}} < p_{t \text{ trig}}$$

$$0.25 < z_1, z_2 < 0.35$$

$$\text{PARP}(91) = 0.7$$

$$\text{PARJ}(21) = 0.4$$

7/31/2012

## Theoretical cuts:

$$Q^2 = 4$$

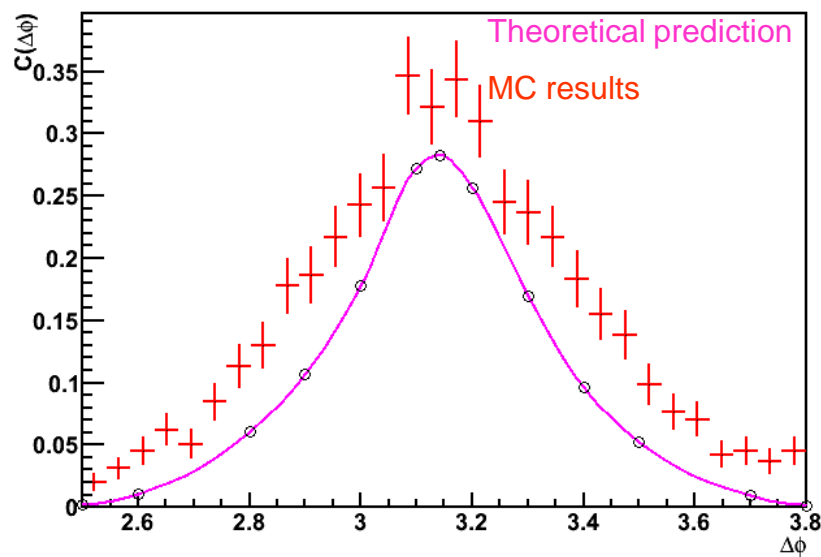
$$y = 0.7$$

$$p_{t \text{ trig}} > 2 \text{ GeV}$$

$$1 < p_{t \text{ asso}} < p_{t \text{ trig}}$$

$$z_1 = z_2 = 0.3$$

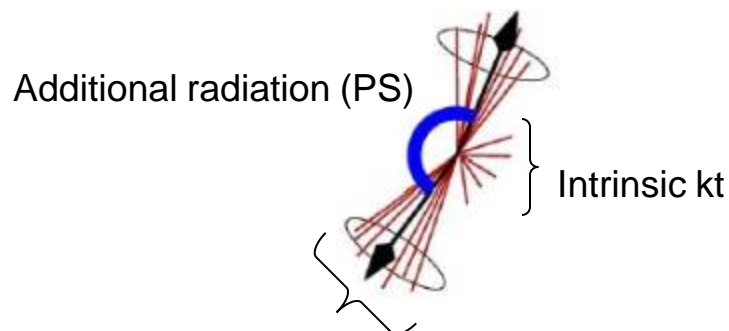
Intrinsic  $k_t = 0.7 \text{ GeV} \sim 0.4 < Q_s^2 < 0.6 \text{ GeV}^2$  in the model  
Fragmentation  $p_t = 0.4 \text{ GeV} \sim \langle p_t^2 \rangle = 0.2 \text{ GeV}^2$  in the model



Theoretical curves from B.W.Xiao

# The power of Monte Carlo

3 factors matter a lot in the decorrelation of back to back jets.



Fragmentation pt

## MC cuts:

$$3.5 < Q^2 < 4.5$$

$$0.65 < y < 0.75$$

$$p_{t \text{ trig}} > 2 \text{ GeV}$$

$$1 < p_{t \text{ asso}} < p_{t \text{ trig}}$$

$$0.25 < z_1, z_2 < 0.35$$

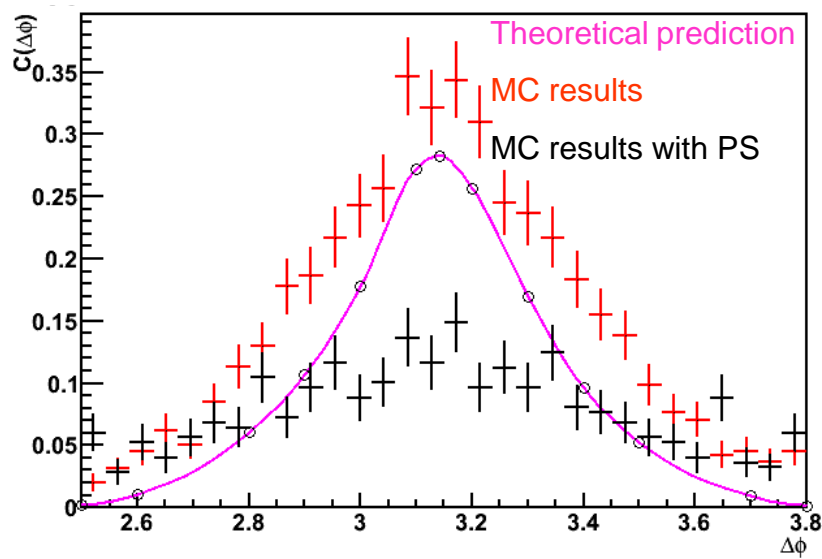
$$\text{PARP}(91) = 0.7$$

$$\text{PARJ}(21) = 0.4$$

7/31/2012

Add PS effect to the theoretical curve

Intrinsic  $k_t = 0.7 \text{ GeV} \sim 0.4 < Q_s^2 < 0.6 \text{ GeV}^2$  in the model  
Fragmentation  $p_t = 0.4 \text{ GeV} \sim \langle p_t^2 \rangle = 0.2 \text{ GeV}^2$  in the model



Theoretical curves from B.W.Xiao